# What extent are visual double stars really binaries to? 

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#### Abstract

On the basis of CCD frames, collected from 2013 till now and obtained with the telescopes of ASV and NAOR, of visual double stars for which there exist orbital or linear elements, we have identified both components in the Gaia DR2 Catalogue. Since that catalogue contains precisely determined parallaxes for both components, we have compared them in order to establish exactly how close to each other they really are in space. Thus, the question of which double stars are really binaries, i.e. gravitationally bound pairs, can be answered more reliably.


Key words: double stars

## Introduction

From the double stars observed at National Astronomical Observatory Rozhen (NAOR) and Astronomical Station Vidojevica (ASV) within 2013 - 2019 we have extracted 179 pairs for which there exist both calculated orbital elements given in the Sixth Catalog of Orbits of Visual Binary Stars (Hartkopf et al. 2001) or linear elements given in the Catalog of Rectilinear Elements (Hartkopf et al. 2011) and Gaia DR2 (Gaia Collaboration et al. 2016,2018 ) parallaxes for both components. Our CCD frames have served to identify pair components in the Gaia DR2 Catalogue.


Fig. 1. The overlapping interval $\Delta \pi$ of parallaxes of double star system. The quantities denoted as $A$ concern the primary, those denoted as $B$ concern the secondary component of a binary.

We compare the component parallaxes $\left(\pi_{A}, \pi_{B}\right)$ including the parallax errors $\left(\sigma_{\pi_{A}}, \sigma_{\pi_{B}}\right)$ and calculate the overlapping interval (Fig. 1) according to the following equation

$$
\begin{equation*}
\Delta \pi=\min \left(\pi_{A}+\sigma_{\pi_{A}}, \pi_{B}+\sigma_{\pi_{B}}\right)-\max \left(\pi_{A}-\sigma_{\pi_{A}}, \pi_{B}-\sigma_{\pi_{B}}\right) \tag{1}
\end{equation*}
$$

In the case of parallax overlapping, i.e. $\Delta \pi>0$, the components may be regarded as sufficiently close to each other so that probably they form a
binary. However, in the case of no overlapping, i.e. $\Delta \pi<0$, the components are mutually distant so that such a pair is most likely optical, i.e. there is no physical binary. This criterion is not sufficient to establish the nature of a double star. Additional criteria, based on analysis of positions, velocities and masses of the components, would have to be used, but such data are available only for a small number of stellar pairs.

## 1 Short statistics of overlapping parallaxes

In our observational material we have segregated 179 stellar pairs for which the parallaxes are given in the Gaia DR2 Catalogue. For 64 of them there are orbital elements available, whereas for 118 ones there are linear elements available. In the case of three pairs there are both orbital and linear elements available.

From the 64 pairs with calculated orbital elements, for $36(56.25 \%)$ parallax overlapping $(\Delta \pi>0)$ has been found, whereas in the case of 28 $(43.75 \%)$ the parallaxes do not overlap $(\Delta \pi<0)$. These 64 pairs are presented in Table 1. WDS designation and discovery designation on whose basis it is possible to identify each pair are given in Columns 1 and 2. Column 3 contains the orbit grade. For the three pairs which also have a linear solution to orbits, grade designation (L) is added. Columns 4-7 contain the parallaxes of the primary $\left(\pi_{A}\right)$, the secondary $\left(\pi_{B}\right)$ and their errors $\left(\sigma_{\pi_{A}}, \sigma_{\pi_{B}}\right)$. In the last column the overlapping value $(\Delta \pi)$, is given which is obtained following relation (1).

As can be seen from Table 1, for most of the orbits the grade is 4 or 5 . According to the Worley-Heintz criterion (as quoted from the Fourth Cata$\log$ grade 4 is "preliminary = individual elements entitled to little weight, and may be subject to substantial revisions". Grade 5 is "indeterminate $=$ the elements may not even be approximately correct. The observed arc is usually too short, with little curvature, and frequently there are large residuals associated with the computations". In Table 1 there are three binaries where the grade of orbital elements is 2 , "good $=$ most of a revolution, well observed, with sufficient curvature to give considerable confidence in the derived elements. No major changes in the elements likely". In other words, we are sure that in the case of a pair with grade 2 the components are gravitationally bound. A simple calculation shows that if we used the $3 \sigma$ rule, the parallaxes would overlap.

A similar conclusion is also valid for the only one binary from Table 1 where the grade is 3 , meaning "reliable $=$ at least half of the orbit defined, but the lesser coverage (in number or distribution) or data consistency leaves the possibility of larger errors than in Grade 2".

From the 118 pairs with linear elements, for $112(94.92 \%)$ there is no parallax overlapping, as could be expected in the case of linear pairs, whereas for six $6(5.08 \%)$ the parallaxes overlap. These pairs are given in Table 2. In order to examine the overlapping of parallaxes (distances), once more, we have also used the catalogue by Bailer-Jones et al. (2018) - "Distances to 1.33 billion stars in Gaia DR2". The columns in the upper part of Table 2 are the same as in Table 1, only that of orbits grade is omitted,
whereas in the lower part of Table 2 the minimum $r_{l o}$ and maximum $r_{h i}$ distances of the components

Table 1. Double stars which have calculated orbital elements.

| WDS | Discover | Orbit |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| designation | designation |  | (mas) | (mas) | (mas) | (mas) | (mas) |
| 00057 + 4549 | ST" 547 AB | 4 | 86.8735 | 0.0484 | 86.9402 | 0.0588 | 0.0405 |
| $00152+2722$ | J 868 | 5, L | 1.8935 | 0.0527 | 3.5488 | 0.0441 | -1.5585 |
| $00321+6715$ | VYS 2AB | 5 | 101.4335 | 0.4733 | 100.4054 | 0.0701 | -0.4847 |
| $00521+1036$ | STF 67 | 4 | 8.9917 | 0.0549 | 8.9372 | 0.3136 | 0.1098 |
| $01032+2006$ | LDS 873 | 5 | 62.6270 | 0.0425 | 62.1000 | 0.2033 | -0.2812 |
| $01467+3310$ | STF 158AB | 5 | 9.6544 | 0.0469 | 9.5512 | 0.1216 | 0.0653 |
| $02291+6724$ | STF 262 AB | 5 | 21.9604 | 0.3332 | 21.7036 | 0.1392 | 0.2156 |
| $03122+3713$ | STF 360 | 4, L | 24.4423 | 0.6554 | 20.5747 | 0.0873 | -3.1249 |
| $03162+5810$ | MLB 115 AB | 5 | 73.7645 | 0.0442 | 73.7407 | 0.0417 | 0.0621 |
| 03368 + 0035 | STF 422 | 5 | 33.7528 | 0.0866 | 33.7882 | 0.0703 | 0.1215 |
| $04076+3804$ | STT 531AB | 5 | 47.2101 | 0.0527 | 47.1305 | 0.2613 | 0.1054 |
| $04367+1930$ | STF 567 | 4 | 15.0064 | 0.0503 | 14.8835 | 0.0419 | -0.0307 |
| $05013+5015$ | STF 619 | 5 | 4.3061 | 0.0372 | 4.5958 | 0.0375 | -0.2150 |
| $05364+2200$ | STF 742 | 5 | 12.4603 | 0.1007 | 13.1274 | 0.0495 | -0.5169 |
| $05535+3720$ | BU 1053 | 5 | 15.0035 | 0.0523 | 15.0920 | 0.0612 | 0.0250 |
| $07106+1543$ | J 703 | 5, L | 2.7841 | 0.0389 | 12.1025 | 0.0391 | -9.2404 |
| $08095+3213$ | STF1187AB | 5 | 11.3335 | 0.7306 | 13.9676 | 0.0548 | -1.8487 |
| $08122+1739$ | STF1196AB, C | 4 | 41.2987 | 0.1710 | 42.1256 | 0.4798 | -0.1761 |
| $09013+1516$ | STF1300AB | 4 | 54.1310 | 0.0416 | 54.2762 | 0.0528 | -0.0508 |
| $09144+5241$ | STF1321AB | 4 | 157.8796 | 0.0366 | 157.8851 | 0.0414 | 0.0725 |
| $09273+0614$ | STF1355 | 4 | 18.7804 | 0.0900 | 18.5979 | 0.0918 | -0.0007 |
| $09414+3857$ | STF1374AB | 4 | 19.2207 | 0.0528 | 18.5919 | 0.2024 | -0.3736 |
| $09524+2659$ | STF1389 | 4 | 18.8816 | 0.0577 | 18.8412 | 0.0592 | 0.0765 |
| $10110+7508$ | KUI 47 | 5 | 47.4964 | 0.0432 | 47.4612 | 0.0420 | 0.0500 |
| $10227+1521$ | STT 216 | 3 | 34.4535 | 0.0409 | 34.1930 | 0.0684 | -0.1512 |
| $10596+2527$ | AG 342 | 5 | 46.9068 | 0.0457 | 46.9147 | 0.0513 | 0.0891 |
| $11080+5249$ | STF1510 | 5 | 17.5162 | 0.0370 | 17.4440 | 0.0337 | -0.0015 |
| $11387+4507$ | STF1561AB | 5 | 42.7909 | 0.0397 | 43.6091 | 0.1011 | -0.6774 |
| $11390+4109$ | STT 237AB | 4 | 12.4809 | 0.0760 | 12.0542 | 0.0751 | -0.2756 |
| $12244+2535$ | STF1639AB | 4 | 11.6398 | 0.0508 | 11.6948 | 0.0572 | 0.0530 |
| $12272+2701$ | STF1643AB | 4 | 36.4871 | 0.0683 | 36.4672 | 0.0601 | 0.1085 |
| $13120+3205$ | STT 261 | 4 | 13.6916 | 0.0417 | 13.7597 | 0.0414 | 0.0150 |
| $13284+1543$ | STT 266 | 4 | 16.7111 | 0.0626 | 16.8001 | 0.0714 | 0.0450 |
| $13328+1649$ | VYS 6 | 5 | 60.3012 | 0.1130 | 60.3748 | 0.0826 | 0.1220 |
| $13491+2659$ | STF1785 | 2 | 73.9239 | 0.0653 | 74.2043 | 0.0456 | -0.1695 |
| 13550-0804 | STF1788AB | 5 | 28.9580 | 0.0440 | 28.9488 | 0.0527 | 0.0875 |
| $14024+4620$ | SWI 1 | 5 | 89.3872 | 0.0661 | 89.3822 | 0.0557 | 0.1114 |
| $14131+5520$ | STF1820 | 4 | 26.1404 | 0.1500 | 26.0256 | 0.0350 | 0.0700 |
| $14165+2007$ | STF1825 | 5 | 30.0609 | 0.0394 | 30.1035 | 0.0545 | 0.0513 |
| $14336+3535$ | STF1858AB | 5 | 25.3724 | 0.0359 | 25.3706 | 0.0371 | 0.0712 |
| $14410+5757$ | STF1872AB | 5 | 17.8573 | 0.0318 | 17.8652 | 0.0384 | 0.0623 |
| $14514+1906$ | STF1888AB | 2 | 148.5195 | 0.2436 | 148.2131 | 0.0464 | -0.0164 |
| $15245+3723$ | STF1938Ba, Bb | 2 | 27.1525 | 0.0250 | 27.2324 | 0.0276 | -0.0273 |
| $15348+1032$ | STF1954AB | 4 | 15.5728 | 0.6571 | 18.7090 | 0.2536 | -2.2255 |
| 15559-0210 | STF1985 | 5 | 26.0630 | 0.0508 | 26.1413 | 0.0610 | 0.0335 |
| $16133+1332$ | STF2021AB | 4 | 41.1510 | 0.0413 | 41.2592 | 0.0352 | -0.0317 |
| $16147+3352$ | STF2032AB | 4 | 44.1346 | 0.0644 | 44.1475 | 0.0237 | 0.0474 |
| $16160+0721$ | STF2026AB | 3 | 37.1441 | 0.0551 | 37.0752 | 0.0452 | 0.0314 |
| $17053+5428$ | STF2130AB | 4 | 36.7992 | 0.0974 | 36.8008 | 0.0604 | 0.1208 |
| $17248+3044$ | BU 1250 | 5 | 2.3733 | 0.0354 | 2.2556 | 0.0439 | -0.0384 |
| $17386+5546$ | STF2199 | 5 | 8.4420 | 0.0324 | 8.7367 | 0.4002 | 0.0648 |
| $18428+5938$ | STF2398AB | 4 | 283.9489 | 0.0624 | 283.8624 | 0.1065 | 0.0824 |
| $18443+3940$ | STF2382AB | 4 | 17.9665 | 0.2274 | 20.4080 | 0.0507 | -2.1634 |
| $18443+3940$ | STF2383CD | 4 | 20.0603 | 0.1196 | 20.1945 | 0.1275 | 0.1129 |
| $19266+2719$ | STF2525AB | 4 | 16.3459 | 0.0392 | 16.2984 | 0.0448 | 0.0365 |
| $19316+1747$ | STF2536 | 5 | 19.1210 | 0.0572 | 19.1344 | 0.0752 | 0.1144 |
| $19458+2710$ | KUI 95AB | 5 | 94.0139 | 0.0804 | 93.9479 | 0.0756 | 0.0900 |
| $20210+1028$ | J 838 | 5 | 0.9171 | 0.0327 | 2.0803 | 0.0327 | -1.0978 |
| $20462+1554$ | STF2725AB | 4 | 25.3160 | 0.2413 | 26.6012 | 0.0370 | -1.0069 |
| $21208+3227$ | STT 437AB | 4 | 14.0435 | 0.0297 | 14.0463 | 0.0335 | 0.0594 |
| $21289+1105$ | STF2799AB | 4 | 10.2442 | 0.0502 | 10.2079 | 0.0494 | 0.0633 |
| $21370+8255$ | STF2837 | 5 | 21.3366 | 0.3034 | 16.5980 | 0.6373 | -3.7979 |
| $22455+1112$ | BU 711 AB | 5 | 23.0586 | 0.0404 | 23.0108 | 0.0409 | 0.0335 |
| $23317+1956$ | WIR 1AB | 5 | 159.7098 | 0.0827 | 160.0598 | 0.1079 | -0.1594 |

(expressed in parsec instead of the component parallaxes) are given. In the last column the overlapping distances $(\Delta r)$ are given.

From Table 2 (lower part) it is seen that when the distance increases, the overlap interval also increases. This can result in a wrong inference that the stars are gravitationally bound, though this is not the case. WDS14098+0822 $=\mathrm{A} 1098$ can be considered to be an example of the most distant double

Table 2. Double stars which have calculated linear elements, but the parallaxes are congruent.

| WDS Discover <br> designation <br> designation | $\begin{gathered} \pi_{A} \\ (\mathrm{mas}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline \sigma_{\pi_{A}} \\ (\mathrm{mas}) \\ \hline \end{gathered}$ | $\begin{gathered} \pi_{B} \\ \text { (mas) } \\ \hline \end{gathered}$ | $\begin{gathered} \sigma_{\pi_{B}} \\ (\mathrm{mas}) \\ \hline \end{gathered}$ | $\begin{gathered} \Delta \pi \\ (\mathrm{mas}) \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $03401+3407$ STF 425AB | 21.8411 | 0.0658 | 21.7646 | 0.0582 | 0.0475 |
| $12025+2145$ HO 535 | 11.5165 | 0.3809 | 11.4831 | 0.0980 | 0.1960 |
| 12151 - 0715 STF1619AB | 29.3041 | 0.0729 | 29.3916 | 0.0749 | 0.0603 |
| $14098+0822$ A 1098 | 1.2232 | 0.0453 | 1.2483 | 0.0442 | 0.0644 |
| $21330+2043$ STF2804AB | 16.7406 | 0.0479 | 16.7396 | 0.0517 | 0.0958 |
| $22326+0725$ STF2915AB | 4.6630 | 0.0672 | 4.6300 | 0.1079 | 0.1344 |
| WDS Discover | ${ }_{o}(A)$ |  | $r_{l o}(B)$ |  |  |
| designation designation | (pc) | (pc) | (pc) | (pc) | (pc) |
| $03401+3407$ STF 425AB | 45.5871 | 45.8643 | 45.7625 | 46.0094 | 0.1017 |
| $12025+2145$ HO 535 | 83.9828 | 89.7738 | 86.1371 | 87.6280 | 1.4908 |
| 12151 - 0715 STF1619AB | 34.0063 | 34.1770 | 33.9031 | 34.0776 | 0.0712 |
| $14098+0822$ A 1098 | 771.2660 | 829.6147 | 757.1539 | 811.9205 | 40.6545 |
| $21330+2043$ STF2804AB | 59.4613 | 59.8049 | 59.4517 | 59.8221 | 0.3435 |
| $\underline{22326+0725 \text { STF2915AB }}$ | 210.1633 | 216.3198 | 209.9164 | 219.9566 | 6.1564 |

star (in our sample). Its primary is at a distance of $(800.44 \pm 29.17) \mathrm{pc}$, the secondary at $(784.53 \pm 27.38) \mathrm{pc}$. When we compare the distance between the components with the distance determination errors, we find that the components are 15.9 pc apart, whereas the errors are almost twice as large. A similar situation appears for the other pairs from Table 2. However, in order to make a sufficiently reliable judgement whether these pairs are gravitationally bound or not, it would be necessary, as mentioned earlier, in addition to the parallaxes to include relative positions, velocities and masses of the components, but these data are yet mostly unknown.

## 2 Conclusion

For more than $60 \%$ of the pairs from our sample which have calculated orbits, the applied criterion showed that the components are really close in space. This can serve as a indicator that the components are gravitationally bound, i.e. they form a binary system.

On the other hand, this criterion in a much higher percentage (more than $94 \%$ ) indicates that the pairs with linear elements are not gravitationally bound, i.e. that they do not form a binary system.

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## References

Bailer-Jones, C. A. L., Rybizki, J., Fouesneau, M., Mantelet, G., \& Andrae, R., 2018, AJ, 156, 58, 11 pp. http://vizier.u-strasbg.fr/viz-bin/VizieR-3?-source=I/347/gaia2dis

Gaia Collaboration et al. (2016): Description of the Gaia mission (spacecraft, instruments, survey and measurement principles, and operations)
Gaia Collaboration et al. (2018): Summary of the contents and survey properties http://vizier.u-strasbg.fr/viz-bin/VizieR-3?-source=I/345/gaia2
Hartkopf, W.I., Mason, B.D. \& Worley, C.E. 2001, AJ, 122, 3472, http://www.usno.navy.mil/USNO/astrometry/optical-IR-prod/wds/orb6
Hartkopf, W.I., \& Mason, B.D. 2011, Catalog of Rectilinear Elements, published in Second USNO Double Star CD 2006.5 available online at http://www.usno.navy.mil/USNO/astrometry/optical-IR-prod/wds/lin1

