

INVESTIGATION OF THE COMA CLUSTER OF GALAXIES

M. Kalinkov

INTRODUCTION

The study of the morphological, kinematical and dynamical properties of the Coma cluster of galaxies is of great importance for a wide variety of questions. The Coma cluster of galaxies is according to Zwicky's classification [1—3] an example of regular cluster.

The distance modulus of this cluster is only $m-M=30^m.7$ (Stebbins and Whitford [4]), and there exists a possibility for the observation of faint cluster galaxies. The Coma cluster possesses a spherical symmetry, which permits the investigation of its space structure. On the other hand it is possible while studying the Coma cluster to obtain an answer about the tendency towards the clustering of galaxies. The investigation of the Coma cluster is in connection with the Universe age as well as with gravitational influences of large distances.

The position of the Coma cluster center is not determined with a great accuracy. According to Omer, Page and Wilson [5] the co-ordinates of this center are

$$(1) \quad \begin{aligned} \alpha_{1950} &= 12^h 57^m.3 \\ \delta_{1950} &= +28^\circ 24', \end{aligned}$$

while according to Zwicky [1, 2], Abell [6, 7], Shane [8] and Shane and Wirtanen [9] these co-ordinates are

$$(2) \quad \begin{aligned} \alpha_{1950} &= 12^h 57^m.3 \\ \delta_{1950} &= +28^\circ 14'. \end{aligned}$$

It seems that the inaccuracy of the center co-ordinates is not important, but as it was pointed out in our previous papers [10, 11], the differences in δ for the above mentioned two determinations are decisive for the study of the cluster rotation.

According to [5] the angular diameter of the Coma cluster is only $100'$; while according to Zwicky [1—3, 7, 12] its angular diameter is at least $12''$. Abell (f. e. [7]) indicates that the cluster is substantially contained

within an oval region of dimensions 5.4 by 4.3 degrees. Sharov [13] and Noonan [14] after different interpretations of Zwicky's data (in [13] the material used is by Wallenquist [15]), do not support Zwicky's conclusions [1, 2].

Some questions in connection with the structural, kinematical and dynamical properties of the Coma cluster of galaxies are examined in the present paper.

RESULTS OF DIAMETER MEASUREMENTS

The observational material in this study is the print No. 1393 (blue and red) of the National Geographic Society — Palomar Observatory Sky Survey. The center co-ordinates of the print are $\alpha_{1950} = 13^{\text{h}}04^{\text{m}}33^{\text{s}}$ and $\delta_{1950} = +29^{\circ}29'25''$.

The co-ordinates of the Coma cluster center were determined with the help of 12 independent counts of galaxies (cross-sections, as in [16—18]) around the approximately known cluster center. The data from 10 cross-sections (in the squares $3' \times 3'$) conform to the co-ordinates (2). Indeed, the Coma cluster center is located between the two brightest galaxies NGC 4874 and NGC 4889=NGC 4884 which have co-ordinates ([19] and [20]):

$$\text{NGC 4874} \begin{cases} \alpha_{1950} = 12^{\text{h}}57^{\text{m}}.2 \\ \delta_{1950} = +28^{\circ}14' \end{cases}$$

$$\text{NGC 4889=NGC 4884} \begin{cases} \alpha_{1950} = 12^{\text{h}}57^{\text{m}}.7 \\ \delta_{1950} = +28^{\circ}15'. \end{cases}$$

It appears that the cluster center is located at a distance of the separation between these two galaxies, reckoned from NGC 4874 to NGC 4889=NGC 4884. Thus determined the center complies with the condition [2]. In the very center of the cluster a galaxy ($m_0 \approx 18^{\text{m}}$) which is not registered in the Catalogues is located. This galaxy was adopted as the cluster center.

The purpose of our measuring was the determination of the major and minor diameters of all galaxies on the *O* and *E* prints, located in a field with a radius of $60'$ around the central galaxy. The field was divided into 12 sectors (of 30°) and 10 rings of $6'$ each. (The radial reseaux were made in the Workshop for scientific instruments at the Astronomical Section, Bulgarian Academy of Sciences.)

The diameter measuring is carried out with a binocular microscope (used in [21]) with $16\times$ and $56\times$ magnifications. As it is known the image scale of the prints is $67''.1 \text{ mm}^{-1}$. The divisions on our eyepiece micrometer are $3''.355$ for $16\times$ and $0''.959$ for $56\times$.

Major and minor diameters of the galaxies were measured for their peripheral (outer) parts on the *E* and *O* prints, as well as for the corresponding diameters of their nuclei. (A work about the measurement errors with respect to various magnifications is out by Karachentsev [22] but only for counts of the galaxies.)

Thus our measurements permit the obtaining of 16 properties from which one may calculate 8 properties more — quantities for the flattening of ga-

Table 1

| Sectors (Zones) | D_1^0 | D_2^0 | ${}^0D_{12}$ | d_1^0 | d_2^0 | ${}^0d_{12}$ | D_3^0 | D_4^0 | ${}^0D_{34}$ | d_3^0 | d_4^0 | ${}^0d_{34}$ | n_i |
|-----------------|---------|---------|--------------|---------|---------|--------------|---------|---------|--------------|---------|---------|--------------|----------------|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| I(No.1) | 4.3 | 4.0 | 92 | 2.6 | 2.4 | 90 | 17.3 | 15.1 | 88 | 9.2 | 8.5 | 92 | 3, 4, 3, 4 |
| II | 5.9 | 4.7 | 80 | 3.1 | 2.3 | 76 | 19.9 | 16.0 | 85 | 9.5 | 7.2 | 78 | 9, 8, 9, 8 |
| III | 7.3 | 6.2 | 78 | 2.5 | 2.0 | 85 | 34.0 | 26.8 | 76 | 9.6 | 7.8 | 82 | 13 |
| IV | 6.7 | 5.0 | 74 | 3.1 | 2.3 | 77 | 22.1 | 17.8 | 80 | 9.7 | 6.9 | 75 | 8, 7, 8, 8 |
| V | 7.6 | 6.4 | 87 | 2.8 | 2.2 | 78 | 24.3 | 18.8 | 77 | 9.8 | 7.8 | 81 | 7 |
| VI | 6.5 | 4.9 | 76 | 3.6 | 2.6 | 74 | 24.6 | 18.6 | 74 | 10.8 | 8.8 | 81 | 7 |
| VII | 3.9 | 2.8 | 74 | 2.2 | 1.6 | 74 | 13.2 | 10.9 | 81 | 7.3 | 5.6 | 77 | 7, 7, 6, 7 |
| VIII | 12.0 | 8.0 | 67 | 3.5 | 2.2 | 60 | 40.0 | 25.0 | 62 | 10.8 | 6.5 | 58 | 1, 2, 1, 2 |
| IX | 4.5 | 2.9 | 68 | 2.4 | 1.7 | 79 | 18.6 | 15.6 | 86 | 6.7 | 5.3 | 83 | 7 |
| X | 18.6 | 14.5 | 81 | 4.7 | 3.6 | 78 | 62.8 | 56.4 | 85 | 17.0 | 12.9 | 80 | 5, 7, 5, 7 |
| XI | 3.1 | 2.5 | 80 | 1.5 | 1.3 | 89 | 9.0 | 7.2 | 81 | 4.0 | 3.5 | 88 | 4, 3, 4, 3 |
| XII | 8.2 | 7.2 | 90 | 3.5 | 3.0 | 87 | 27.2 | 22.2 | 82 | 10.2 | 9.0 | 87 | 4 |
| I(No.2) | 5.7 | 4.3 | 75 | 2.4 | 1.7 | 83 | 22.8 | 16.9 | 79 | 6.7 | 5.3 | 84 | 9 |
| II | 9.8 | 7.2 | 73 | 3.8 | 2.8 | 80 | 34.5 | 25.7 | 75 | 12.3 | 8.3 | 73 | 6 |
| III | 7.3 | 6.0 | 84 | 3.4 | 2.6 | 81 | 21.5 | 18.1 | 83 | 10.9 | 8.5 | 81 | 9; 10, 11, 10 |
| IV | 4.7 | 3.2 | 74 | 1.8 | 1.3 | 86 | 16.8 | 10.7 | 69 | 5.4 | 4.3 | 88 | 11, 8, 11, 9 |
| V | 5.3 | 4.2 | 81 | 2.8 | 2.2 | 86 | 19.9 | 15.2 | 76 | 9.8 | 8.2 | 83 | 9 |
| VI | 6.0 | 3.2 | 63 | 2.5 | 2.1 | 79 | 21.2 | 11.6 | 66 | 8.6 | 6.3 | 77 | 11 |
| VII | 6.6 | 3.8 | 61 | 3.3 | 2.1 | 62 | 23.6 | 16.3 | 72 | 11.6 | 7.5 | 71 | 7 |
| VIII | 5.5 | 4.2 | 75 | 3.3 | 2.7 | 78 | 19.7 | 14.7 | 75 | 10.0 | 8.0 | 80 | 6, 5, 6, 6 |
| IX | 7.0 | 5.0 | 72 | 3.1 | 2.2 | 75 | 23.3 | 18.8 | 79 | 9.9 | 6.9 | 71 | 10, 9, 10, 9 |
| X | 4.3 | 3.0 | 78 | 2.4 | 1.4 | 72 | 15.4 | 10.9 | 79 | 7.4 | 5.2 | 82 | 11 |
| XI | 8.1 | 6.0 | 73 | 3.6 | 2.8 | 78 | 32.6 | 23.4 | 72 | 11.2 | 8.5 | 77 | 11, 10, 11, 11 |
| XII | 5.4 | 4.6 | 80 | 2.8 | 2.3 | 81 | 17.8 | 15.0 | 83 | 7.7 | 6.2 | 79 | 8 |
| I(No.3) | 7.3 | 4.7 | 66 | 2.4 | 1.9 | 81 | 22.9 | 14.8 | 67 | 6.5 | 5.2 | 80 | 8 |
| II | 11.8 | 5.9 | 59 | 4.4 | 3.1 | 70 | 36.8 | 20.8 | 62 | 15.7 | 10.7 | 72 | 8, 6, 8, 6 |
| III | 6.2 | 5.1 | 80 | 2.6 | 2.0 | 72 | 22.6 | 18.7 | 78 | 7.7 | 6.1 | 77 | 7 |
| IV | 4.8 | 3.5 | 73 | 2.2 | 2.5 | 78 | 18.2 | 11.7 | 67 | 6.3 | 4.6 | 75 | 13 |
| V | 7.3 | 5.0 | 74 | 4.6 | 2.7 | 69 | 30.7 | 20.0 | 72 | 14.3 | 8.8 | 73 | 14, 13, 14, 14 |
| VI | 5.6 | 3.4 | 65 | 2.4 | 1.8 | 77 | 16.7 | 11.0 | 68 | 7.0 | 5.2 | 76 | 7 |
| VII | 8.2 | 4.6 | 64 | 4.0 | 2.1 | 67 | 27.8 | 18.0 | 70 | 12.0 | 7.3 | 74 | 12, 11, 12, 11 |
| VIII | 5.7 | 3.8 | 68 | 3.3 | 1.9 | 60 | 20.0 | 13.0 | 65 | 8.5 | 5.1 | 60 | 5 |
| IX | 7.6 | 4.8 | 65 | 3.3 | 2.1 | 66 | 22.2 | 15.2 | 68 | 10.5 | 7.0 | 72 | 10, 12, 12, 11 |
| X | 10.9 | 6.8 | 72 | 4.4 | 3.1 | 71 | 37.8 | 27.5 | 76 | 14.6 | 10.6 | 78 | 13 |
| XI | 8.3 | 4.1 | 59 | 4.4 | 2.0 | 63 | 28.2 | 15.8 | 67 | 13.6 | 6.5 | 62 | 5 |
| XII | 14.8 | 9.7 | 74 | 4.5 | 3.4 | 76 | 60.7 | 40.7 | 75 | 16.2 | 11.6 | 77 | 6 |
| I(No.4) | 8.1 | 3.8 | 62 | 3.8 | 2.4 | 72 | 25.3 | 15.1 | 69 | 8.2 | 5.6 | 71 | 9, 9, 9, 8 |
| II | 6.9 | 4.4 | 67 | 3.2 | 2.2 | 70 | 24.4 | 16.9 | 70 | 9.2 | 6.3 | 71 | 9 |
| III | 9.1 | 5.9 | 61 | 3.1 | 2.3 | 72 | 27.4 | 19.6 | 69 | 11.1 | 8.4 | 72 | 7 |
| IV | 6.4 | 4.0 | 72 | 2.4 | 2.0 | 77 | 21.5 | 14.9 | 74 | 8.2 | 6.4 | 82 | 10, 12, 12, 12 |
| V | 8.4 | 5.8 | 68 | 3.5 | 2.4 | 71 | 30.4 | 22.2 | 74 | 11.0 | 8.1 | 72 | 6 |
| VI | 7.4 | 5.6 | 77 | 4.4 | 3.4 | 81 | 26.8 | 22.2 | 83 | 13.4 | 11.0 | 85 | 5 |
| VII | 7.1 | 5.1 | 77 | 3.6 | 2.4 | 73 | 23.9 | 18.1 | 80 | 9.7 | 7.4 | 75 | 7, 6, 7, 7 |
| VIII | 8.1 | 5.6 | 69 | 4.2 | 3.2 | 73 | 28.6 | 24.3 | 79 | 14.2 | 10.7 | 67 | 7, 6, 7, 6 |
| IX | 14.3 | 10.9 | 78 | 4.3 | 3.0 | 75 | 47.9 | 41.7 | 84 | 14.1 | 9.8 | 74 | 9 |
| X | 4.6 | 3.0 | 63 | 2.5 | 1.8 | 71 | 17.8 | 13.4 | 75 | 7.7 | 5.0 | 64 | 7 |
| XI | 8.0 | 6.2 | 71 | 3.2 | 1.9 | 70 | 19.7 | 17.0 | 78 | 9.9 | 6.0 | 68 | 4, 6, 6, 6 |
| XII | 5.2 | 3.5 | 71 | 2.4 | 1.4 | 65 | 17.2 | 12.2 | 71 | 6.6 | 3.8 | 60 | 8, 6, 8, 6 |

Continued — table 1

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|---------|------|-----|----|-----|-----|----|------|------|----|------|------|----|----------------|----|
| I(No.5) | 5.8 | 3.0 | 56 | 2.4 | 1.8 | 73 | 14.4 | 9.5 | 68 | 6.9 | 4.5 | 67 | 7, 7, 8, 8 | |
| II | 11.4 | 5.2 | 53 | 4.2 | 2.3 | 64 | 35.1 | 17.6 | 57 | 14.5 | 7.7 | 61 | 9 | |
| III | 8.4 | 4.9 | 67 | 3.4 | 2.6 | 75 | 24.3 | 17.3 | 75 | 8.1 | 6.3 | 78 | 9 | |
| IV | 9.1 | 4.8 | 61 | 3.8 | 2.2 | 64 | 32.6 | 15.7 | 56 | 11.5 | 6.4 | 65 | 11 | |
| V | 7.9 | 5.2 | 64 | 4.4 | 2.7 | 62 | 32.0 | 21.7 | 66 | 14.1 | 8.4 | 59 | 7 | |
| VI | 6.1 | 3.7 | 60 | 4.0 | 2.2 | 58 | 20.8 | 12.3 | 59 | 10.2 | 6.9 | 68 | 6, 4, 6, 4 | |
| VII | 7.7 | 4.6 | 68 | 3.6 | 2.5 | 76 | 26.6 | 17.6 | 70 | 12.9 | 8.5 | 73 | 9, 8, 9, 8 | |
| VIII | 9.0 | 4.2 | 49 | 3.6 | 2.2 | 61 | 28.7 | 15.0 | 52 | 10.4 | 6.2 | 64 | 6, 7, 6, 7 | |
| IX | 11.4 | 7.2 | 59 | 4.1 | 2.7 | 65 | 35.4 | 30.8 | 80 | 11.6 | 9.3 | 74 | 5 | |
| X | 7.6 | 4.9 | 71 | 4.3 | 2.6 | 64 | 29.9 | 20.4 | 69 | 14.6 | 9.0 | 62 | 7, 5, 7, 5 | |
| XI | 9.1 | 5.9 | 61 | 4.2 | 2.4 | 69 | 28.1 | 19.4 | 67 | 13.1 | 8.1 | 68 | 7 | |
| XII | 7.5 | 4.9 | 68 | 3.9 | 2.4 | 63 | 26.5 | 18.4 | 66 | 13.2 | 8.2 | 63 | 5, 6, 6, 6 | |
| I(No.6) | 6.8 | 4.3 | 65 | 3.1 | 1.8 | 60 | 23.9 | 16.3 | 67 | 9.5 | 6.4 | 66 | 11, 10, 11, 10 | |
| II | 6.0 | 3.3 | 54 | 1.9 | 1.0 | 53 | 19.5 | 10.7 | 54 | 6.6 | 3.8 | 58 | 5, 6, 6, 6 | |
| III | 7.5 | 4.5 | 62 | 3.8 | 2.0 | 52 | 26.2 | 15.5 | 64 | 12.3 | 6.7 | 58 | 6, 5, 6, 6 | |
| IV | 7.3 | 5.2 | 71 | 4.1 | 2.4 | 62 | 25.1 | 16.8 | 68 | 11.4 | 7.0 | 63 | 9 | |
| V | 6.7 | 4.6 | 69 | 3.5 | 2.5 | 70 | 25.9 | 18.5 | 67 | 11.0 | 8.2 | 73 | 10 | |
| VI | 8.3 | 4.8 | 67 | 4.7 | 2.2 | 52 | 27.7 | 17.3 | 67 | 15.7 | 7.2 | 55 | 3 | |
| VII | 6.2 | 5.0 | 79 | 3.2 | 2.6 | 79 | 18.5 | 16.5 | 89 | 9.0 | 7.2 | 80 | 4 | |
| VIII | 9.3 | 6.8 | 72 | 3.8 | 2.7 | 72 | 30.9 | 24.3 | 75 | 12.2 | 8.6 | 71 | 9, 8, 9, 8 | |
| IX | 6.2 | 2.9 | 56 | 2.9 | 1.6 | 60 | 19.4 | 10.3 | 59 | 9.7 | 5.3 | 60 | 7, 7, 7, 6 | |
| X | 8.2 | 6.0 | 76 | 4.1 | 2.6 | 68 | 26.4 | 18.8 | 70 | 12.1 | 8.5 | 72 | 8, 7, 8, 7 | |
| XI | 4.8 | 3.2 | 69 | 2.3 | 1.6 | 69 | 15.8 | 9.7 | 66 | 6.5 | 4.6 | 70 | 9 | |
| XII | 5.9 | 3.7 | 63 | 2.9 | 1.5 | 72 | 20.3 | 12.8 | 69 | 9.6 | 5.4 | 71 | 9, 8, 9, 8 | |
| I(No.7) | 6.2 | 3.1 | 53 | 2.4 | 1.9 | 81 | 22.7 | 12.3 | 53 | 7.1 | 5.5 | 80 | 7 | |
| II | 5.8 | 3.2 | 60 | 2.2 | 1.6 | 81 | 18.5 | 11.4 | 64 | 6.8 | 4.8 | 73 | 7, 8, 8, 8 | |
| III | 6.2 | 4.9 | 75 | 2.4 | 1.9 | 76 | 20.9 | 17.6 | 82 | 8.6 | 6.3 | 73 | 9 | |
| IV | 6.6 | 3.8 | 62 | 2.8 | 1.8 | 68 | 22.9 | 13.9 | 63 | 8.8 | 5.5 | 66 | 10 | |
| V | 10.8 | 6.2 | 66 | 4.8 | 3.0 | 66 | 43.6 | 26.9 | 64 | 16.1 | 9.6 | 61 | 16 | |
| VI | 5.2 | 3.2 | 65 | 3.0 | 1.8 | 60 | 19.2 | 13.0 | 67 | 8.8 | 5.9 | 67 | 6, 6, 6, 5 | |
| VII | 10.4 | 6.4 | 62 | 3.6 | 2.4 | 74 | 35.3 | 23.6 | 67 | 11.9 | 8.2 | 73 | 7 | |
| VIII | 9.2 | 6.2 | 64 | 3.6 | 2.5 | 74 | 28.2 | 18.8 | 63 | 11.0 | 8.0 | 74 | 4 | |
| IX | 6.4 | 4.1 | 66 | 3.9 | 2.2 | 58 | 23.3 | 15.7 | 70 | 11.9 | 7.2 | 62 | 7, 5, 7, 5 | |
| X | 8.7 | 6.1 | 70 | 4.2 | 2.8 | 74 | 28.1 | 22.3 | 79 | 12.3 | 9.4 | 79 | 11, 10, 11, 10 | |
| XI | 7.1 | 4.9 | 69 | 3.3 | 2.3 | 70 | 25.5 | 15.2 | 61 | 10.3 | 6.7 | 63 | 10, 9, 10, 9 | |
| XII | 5.4 | 4.3 | 78 | 1.9 | 1.4 | 77 | 17.2 | 12.6 | 71 | 6.7 | 4.7 | 72 | 9 | |
| I(No.8) | 9.2 | 4.6 | 59 | 3.0 | 1.8 | 73 | 26.2 | 14.0 | 60 | 7.3 | 4.5 | 69 | 4, 3, 4, 3 | |
| II | 8.9 | 5.3 | 58 | 3.7 | 2.5 | 61 | 33.1 | 21.2 | 57 | 12.1 | 7.9 | 57 | 9, 8, 9, 8 | |
| III | 6.2 | 4.6 | 73 | 2.8 | 1.8 | 63 | 23.0 | 16.7 | 74 | 12.8 | 8.6 | 63 | 5 | |
| IV | 7.2 | 4.9 | 63 | 3.4 | 2.2 | 61 | 29.7 | 19.2 | 60 | 11.5 | 7.5 | 62 | 10 | |
| V | 9.4 | 4.7 | 54 | 3.3 | 2.3 | 69 | 35.8 | 19.6 | 55 | 11.1 | 7.4 | 62 | 9 | |
| VI | 7.0 | 4.0 | 55 | 4.0 | 2.5 | 59 | 25.0 | 14.0 | 54 | 12.2 | 7.0 | 53 | 4 | |
| VII | 7.4 | 5.1 | 76 | 3.2 | 2.2 | 73 | 21.0 | 15.3 | 73 | 8.8 | 6.8 | 77 | 6, 6, 7, 6 | |
| VIII | 6.0 | 4.2 | 71 | 2.5 | 1.6 | 66 | 20.8 | 14.6 | 74 | 7.1 | 4.9 | 68 | 5, 4, 5, 4 | |
| IX | 4.6 | 3.2 | 76 | 2.6 | 1.5 | 60 | 16.7 | 11.6 | 72 | 9.4 | 5.8 | 63 | 8, 8, 8, 7 | |
| X | 13.0 | 6.2 | 56 | 4.8 | 2.2 | 57 | 45.6 | 19.1 | 49 | 15.5 | 7.5 | 61 | 9 | |
| XI | 8.5 | 4.7 | 63 | 4.3 | 2.2 | 61 | 29.8 | 17.8 | 66 | 13.5 | 7.0 | 63 | 5 | |
| XII | 5.5 | 3.8 | 72 | 2.8 | 1.7 | 60 | 18.2 | 13.3 | 76 | 7.2 | 4.6 | 65 | 6 | |
| I(No.9) | 9.0 | 4.4 | 60 | 4.9 | 2.5 | 67 | 34.0 | 17.6 | 64 | 15.1 | 8.1 | 70 | 7 | |
| II | 5.0 | 2.5 | 52 | 1.4 | 1.2 | 88 | 19.0 | 9.8 | 52 | 5.4 | 4.1 | 74 | 5 | |
| III | 7.9 | 4.7 | 61 | 3.4 | 2.4 | 66 | 27.1 | 18.0 | 67 | 9.9 | 5.7 | 59 | 7 | |
| IV | 12.1 | 7.2 | 64 | 4.4 | 3.1 | 71 | 41.8 | 32.6 | 75 | 14.6 | 10.6 | 74 | 9 | |
| V | 9.3 | 3.8 | 46 | 3.8 | 2.3 | 71 | 32.3 | 15.3 | 49 | 13.3 | 7.3 | 61 | 3 | |
| VI | 10.1 | 6.6 | 68 | 6.5 | 2.8 | 60 | 35.0 | 25.6 | 74 | 15.5 | 9.4 | 63 | 8 | |
| VII | 5.8 | 3.8 | 64 | 2.6 | 1.8 | 68 | 20.5 | 13.5 | 68 | 7.1 | 5.0 | 70 | 4 | |

Continued—table 1

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|---------|------|-----|----|-----|-----|----|------|------|----|------|------|----|----------------|
| VIII | 6.0 | 3.5 | 61 | 3.2 | 1.9 | 60 | 22.4 | 13.8 | 63 | 7.4 | 5.6 | 76 | 8, 10, 9, 10 |
| IX | 5.6 | 3.4 | 59 | 2.8 | 1.6 | 59 | 16.8 | 12.5 | 73 | 9.1 | 6.0 | 66 | 4 |
| X | 7.6 | 5.2 | 68 | 3.7 | 2.3 | 64 | 29.2 | 20.9 | 70 | 11.3 | 7.7 | 68 | 16, 15, 16, 15 |
| XI | 5.4 | 3.3 | 65 | 2.6 | 1.6 | 64 | 18.4 | 10.9 | 63 | 7.7 | 4.6 | 63 | 6, 7, 7, 7 |
| XII | 9.2 | 7.1 | 74 | 4.2 | 3.3 | 84 | 32.8 | 19.9 | 63 | 12.7 | 10.2 | 85 | 6, 5, 6, 5 |
| (No.10) | 5.9 | 5.0 | 79 | 2.4 | 1.8 | 78 | 22.7 | 17.1 | 73 | 8.2 | 6.1 | 76 | 7 |
| II | 9.2 | 6.0 | 65 | 4.4 | 2.2 | 57 | 26.2 | 17.5 | 70 | 13.0 | 7.0 | 56 | 4 |
| III | 8.6 | 4.0 | 58 | 3.8 | 2.1 | 64 | 32.2 | 14.8 | 58 | 10.0 | 6.4 | 66 | 4 |
| IV | 11.0 | 6.5 | 55 | 3.6 | 2.5 | 78 | 37.2 | 22.1 | 61 | 13.6 | 8.4 | 72 | 8 |
| V | 10.0 | 6.6 | 68 | 3.7 | 2.7 | 73 | 32.5 | 22.2 | 73 | 11.3 | 7.2 | 67 | 4, 3, 4, 3 |
| VI | 6.8 | 3.5 | 62 | 2.7 | 1.9 | 69 | 17.8 | 11.3 | 70 | 6.7 | 5.2 | 78 | 6 |
| VII | 6.4 | 4.7 | 76 | 3.2 | 2.4 | 76 | 22.6 | 17.4 | 78 | 10.0 | 7.4 | 77 | 7 |
| VIII | 8.0 | 4.7 | 66 | 3.3 | 2.3 | 71 | 28.2 | 17.4 | 67 | 10.4 | 6.4 | 63 | 7, 7, 5, 7 |
| IX | 6.1 | 3.9 | 64 | 2.8 | 1.7 | 61 | 21.0 | 14.2 | 68 | 9.4 | 5.9 | 63 | 5 |
| X | 8.4 | 5.6 | 72 | 3.9 | 2.0 | 70 | 30.1 | 18.4 | 69 | 12.9 | 7.1 | 66 | 14, 13, 14, 13 |
| XI | 5.8 | 2.9 | 55 | 3.0 | 1.6 | 61 | 20.4 | 11.2 | 62 | 10.0 | 5.2 | 71 | 7, 7, 8, 6 |
| XII | 6.9 | 3.1 | 63 | 2.8 | 1.6 | 57 | 23.0 | 13.4 | 59 | 8.7 | 5.3 | 62 | 9 |

| | D_1^E | D_2^E | $\epsilon_{D_1}^E$ | d_1^E | d_2^E | $\epsilon_{d_1}^E$ | D_3^E | D_4^E | $\epsilon_{D_3}^E$ | d_3^E | d_4^E | $\epsilon_{d_3}^E$ | n_t |
|---------|---------|---------|--------------------|---------|---------|--------------------|---------|---------|--------------------|---------|---------|--------------------|----------------|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| I(No.1) | 5.0 | 4.3 | 86 | 2.6 | 2.1 | 81 | 16.0 | 14.5 | 89 | 8.5 | 7.8 | 90 | 3, 4, 4, 4 |
| II | 6.1 | 4.6 | 79 | 3.1 | 2.3 | 76 | 19.7 | 16.2 | 86 | 9.1 | 7.9 | 87 | 7, 9, 9, 9 |
| III | 12.9 | 10.7 | 80 | 2.7 | 2.3 | 86 | 45.9 | 38.6 | 78 | 9.6 | 8.0 | 85 | 8, 13, 8, 13 |
| IV | 8.2 | 6.1 | 76 | 3.4 | 2.6 | 82 | 25.3 | 20.4 | 84 | 11.6 | 8.3 | 82 | 6, 7, 7, 7 |
| V | 8.7 | 6.8 | 81 | 3.1 | 2.5 | 83 | 22.7 | 18.6 | 79 | 9.6 | 8.2 | 86 | 6, 7, 7, 7 |
| VI | 6.8 | 4.8 | 72 | 3.6 | 2.8 | 79 | 23.0 | 18.8 | 81 | 11.2 | 8.8 | 78 | 6 |
| VII | 4.1 | 2.9 | 70 | 2.3 | 1.8 | 80 | 15.5 | 12.0 | 79 | 7.2 | 5.4 | 81 | 5, 6, 3, 6 |
| VIII | 12.0 | 5.0 | 33 | 3.2 | 2.2 | 71 | 42.0 | 26.0 | 62 | 11.5 | 7.5 | 52 | 1, 2, 1, 2 |
| IX | 3.7 | 3.0 | 81 | 2.0 | 1.6 | 82 | 15.5 | 12.8 | 84 | 6.5 | 5.2 | 79 | 6 |
| X | 16.4 | 12.8 | 85 | 4.9 | 3.9 | 88 | 58.6 | 50.2 | 94 | 16.9 | 13.8 | 88 | 5, 7, 5, 7 |
| XI | 3.0 | 2.8 | 93 | 1.6 | 1.5 | 94 | 10.0 | 9.0 | 90 | 4.2 | 3.4 | 80 | 4, 4, 5, 4 |
| XII | 7.6 | 6.0 | 78 | 3.6 | 2.8 | 82 | 28.0 | 21.2 | 78 | 13.1 | 10.8 | 84 | 4 |
| I(No.2) | 5.1 | 4.1 | 88 | 2.2 | 1.8 | 90 | 18.6 | 14.7 | 84 | 6.3 | 5.2 | 94 | 8, 9, 9, 9 |
| II | 9.8 | 6.9 | 74 | 3.7 | 2.2 | 64 | 28.5 | 22.7 | 79 | 12.7 | 8.1 | 71 | 6 |
| III | 6.9 | 6.1 | 91 | 3.7 | 2.9 | 81 | 23.3 | 19.5 | 84 | 11.7 | 9.4 | 82 | 8, 9, 10, 9 |
| IV | 3.8 | 2.7 | 76 | 1.7 | 1.2 | 85 | 14.4 | 9.5 | 71 | 5.5 | 4.2 | 82 | 11, 10, 11, 11 |
| V | 5.2 | 4.3 | 85 | 2.4 | 2.1 | 84 | 16.7 | 13.9 | 85 | 8.1 | 6.9 | 89 | 7, 9, 9, 9 |
| VI | 6.1 | 3.2 | 62 | 2.7 | 2.2 | 85 | 19.1 | 10.9 | 67 | 8.0 | 6.4 | 82 | 10, 11, 11, 11 |
| VII | 5.6 | 3.1 | 61 | 2.6 | 1.8 | 70 | 17.9 | 11.3 | 66 | 10.2 | 7.7 | 75 | 10, 9, 10, 7 |
| VIII | 5.8 | 4.9 | 84 | 3.4 | 2.4 | 69 | 19.2 | 14.6 | 76 | 10.6 | 7.4 | 71 | 5 |
| IX | 6.5 | 4.7 | 72 | 3.3 | 2.3 | 73 | 21.1 | 18.0 | 81 | 10.6 | 6.5 | 74 | 9 |
| X | 5.3 | 3.4 | 82 | 2.3 | 1.5 | 72 | 16.8 | 11.7 | 80 | 9.2 | 5.9 | 81 | 6, 7, 7, 6 |
| XI | 8.2 | 5.0 | 63 | 3.3 | 2.4 | 75 | 28.1 | 19.7 | 70 | 11.1 | 8.5 | 74 | 11 |
| XII | 4.7 | 3.8 | 82 | 2.8 | 2.2 | 77 | 16.8 | 14.2 | 86 | 8.0 | 7.2 | 88 | 8, 6, 8, 6 |
| I(No.3) | 6.2 | 4.1 | 66 | 2.3 | 1.8 | 80 | 20.1 | 14.6 | 67 | 6.4 | 5.2 | 83 | 8 |
| II | 10.4 | 6.1 | 62 | 4.6 | 3.0 | 68 | 36.0 | 21.9 | 61 | 16.7 | 11.0 | 70 | 8, 6, 8, 6 |
| III | 6.2 | 4.7 | 74 | 2.2 | 1.7 | 68 | 18.5 | 14.8 | 76 | 7.3 | 5.8 | 76 | 5, 6, 6, 6 |
| IV | 4.2 | 3.2 | 80 | 1.9 | 1.6 | 85 | 14.7 | 11.4 | 79 | 6.0 | 4.5 | 78 | 12 |
| V | 8.9 | 5.2 | 69 | 4.2 | 2.4 | 76 | 29.0 | 17.4 | 66 | 15.7 | 9.5 | 72 | 13, 14, 14, 13 |
| VI | 4.0 | 2.7 | 73 | 2.1 | 1.6 | 90 | 14.0 | 10.3 | 76 | 6.0 | 4.6 | 77 | 7 |
| VII | 7.2 | 4.3 | 68 | 3.5 | 2.2 | 72 | 25.4 | 14.4 | 62 | 11.4 | 7.4 | 76 | 12, 11, 12, 11 |

Continued — table 1

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|---------|------|-----|----|-----|-----|----|------|------|-----|------|------|----|----------------|
| VIII | 5.5 | 3.5 | 66 | 2.6 | 1.8 | 69 | 18.0 | 11.2 | 66 | 8.0 | 5.6 | 74 | 5 |
| IX | 7.2 | 4.8 | 71 | 3.9 | 2.4 | 74 | 23.3 | 15.9 | 71 | 11.2 | 7.5 | 72 | 10, 11, 11, 11 |
| X | 9.4 | 6.5 | 73 | 4.4 | 3.3 | 84 | 32.3 | 22.5 | 74 | 14.9 | 10.2 | 74 | 13 |
| XI | 7.2 | 3.7 | 61 | 4.4 | 1.9 | 57 | 23.4 | 14.0 | 69 | 13.1 | 6.0 | 58 | 5 |
| XII | 12.2 | 7.6 | 68 | 5.1 | 3.2 | 74 | 51.0 | 29.3 | 70 | 17.2 | 11.2 | 73 | 6 |
| I(No.4) | 6.2 | 3.7 | 71 | 2.7 | 1.7 | 66 | 23.1 | 12.7 | 69 | 7.9 | 4.8 | 70 | 9 |
| II | 6.4 | 4.6 | 75 | 2.9 | 1.8 | 64 | 20.8 | 15.4 | 76 | 8.3 | 5.5 | 69 | 9 |
| III | 7.4 | 4.7 | 63 | 3.2 | 2.1 | 60 | 24.7 | 15.0 | 59 | 10.7 | 6.7 | 60 | 6, 7, 7, 7 |
| IV | 5.3 | 3.3 | 69 | 2.3 | 1.8 | 80 | 20.3 | 12.3 | 61 | 7.8 | 5.6 | 77 | 11, 12, 12, 12 |
| V | 8.6 | 6.0 | 74 | 3.2 | 2.5 | 77 | 29.8 | 23.4 | 74 | 11.4 | 8.0 | 70 | 5 |
| VI | 7.6 | 6.3 | 81 | 3.5 | 2.9 | 82 | 23.6 | 20.2 | 83 | 10.0 | 8.9 | 82 | 5 |
| VII | 5.8 | 3.9 | 70 | 3.0 | 2.3 | 80 | 19.7 | 13.1 | 69 | 10.2 | 7.5 | 74 | 7, 6, 7, 6 |
| VIII | 8.0 | 5.2 | 63 | 3.8 | 2.8 | 77 | 26.0 | 19.6 | 70 | 15.2 | 10.7 | 66 | 7, 6, 7, 6 |
| IX | 12.6 | 9.3 | 79 | 4.3 | 2.9 | 71 | 40.4 | 34.0 | 83 | 14.7 | 10.4 | 78 | 9 |
| X | 4.4 | 3.1 | 72 | 2.5 | 1.9 | 77 | 17.5 | 12.2 | 70 | 7.4 | 5.8 | 79 | 6 |
| XI | 6.2 | 4.9 | 78 | 3.2 | 1.9 | 74 | 20.7 | 16.2 | 77 | 12.0 | 6.8 | 71 | 6, 5, 6, 5 |
| XII | 4.3 | 2.9 | 67 | 1.9 | 1.2 | 64 | 16.2 | 10.5 | 66 | 6.1 | 3.8 | 64 | 8 |
| I(No.5) | 4.9 | 2.9 | 60 | 2.4 | 1.1 | 52 | 15.4 | 9.4 | 63 | 6.5 | 3.9 | 65 | 7, 8, 8, 8 |
| II | 10.7 | 4.8 | 57 | 4.6 | 2.3 | 63 | 32.2 | 14.9 | 57 | 14.4 | 7.6 | 63 | 8, 7, 8, 7 |
| III | 7.1 | 4.5 | 68 | 2.3 | 1.7 | 73 | 21.4 | 14.8 | 70 | 7.8 | 6.3 | 80 | 9 |
| IV | 8.1 | 4.4 | 64 | 3.5 | 2.7 | 68 | 24.8 | 14.4 | 64 | 11.1 | 6.5 | 64 | 11 |
| V | 7.6 | 5.3 | 72 | 4.5 | 2.9 | 66 | 29.1 | 20.0 | 66 | 15.5 | 9.5 | 62 | 7, 6, 7, 6 |
| VI | 5.8 | 3.4 | 58 | 2.4 | 1.5 | 61 | 18.5 | 9.5 | 54 | 9.5 | 5.6 | 60 | 6, 6, 6, 4 |
| VII | 7.1 | 4.3 | 65 | 3.6 | 2.2 | 64 | 22.7 | 16.2 | 75 | 11.8 | 7.6 | 71 | 9 |
| VIII | 7.2 | 3.8 | 52 | 3.2 | 1.9 | 65 | 24.4 | 14.0 | 58 | 9.6 | 5.7 | 64 | 6, 7, 7, 7 |
| IX | 12.5 | 8.9 | 68 | 5.1 | 3.2 | 64 | 36.2 | 27.8 | 74 | 16.2 | 11.2 | 66 | 4 |
| X | 7.2 | 4.5 | 69 | 4.4 | 2.3 | 62 | 27.3 | 17.7 | 74 | 12.3 | 7.5 | 66 | 7, 5, 7, 6 |
| XI | 8.4 | 5.1 | 62 | 4.0 | 2.6 | 69 | 29.7 | 18.6 | 61 | 13.1 | 8.3 | 66 | 7 |
| XII | 7.3 | 5.1 | 72 | 4.8 | 3.2 | 72 | 25.3 | 18.9 | 71 | 16.5 | 10.0 | 66 | 5, 4, 6, 4 |
| I(No.6) | 5.8 | 3.4 | 59 | 2.6 | 1.8 | 66 | 22.0 | 12.5 | 58 | 9.6 | 6.7 | 67 | 11, 10, 11, 8 |
| II | 5.1 | 3.0 | 61 | 2.1 | 1.1 | 57 | 16.0 | 9.3 | 60 | 5.5 | 3.1 | 58 | 6 |
| III | 8.1 | 4.2 | 58 | 4.5 | 2.1 | 50 | 27.0 | 15.8 | 62 | 14.0 | 7.6 | 63 | 5, 4, 5, 5 |
| IV | 7.1 | 4.1 | 58 | 3.2 | 1.8 | 58 | 22.7 | 15.3 | 67 | 9.0 | 5.7 | 61 | 9 |
| V | 5.8 | 4.8 | 81 | 3.3 | 2.6 | 76 | 23.3 | 17.3 | 72 | 9.9 | 8.0 | 80 | 10 |
| VI | 8.2 | 3.8 | 49 | 4.0 | 2.2 | 59 | 27.8 | 15.7 | 57 | 13.0 | 7.7 | 61 | 3 |
| VII | 4.8 | 3.8 | 73 | 2.1 | 1.9 | 91 | 17.7 | 17.7 | 100 | 8.2 | 7.1 | 87 | 4, 4, 3, 4 |
| VIII | 9.3 | 6.2 | 61 | 3.6 | 2.6 | 68 | 30.9 | 22.2 | 66 | 11.9 | 8.2 | 66 | 9, 8, 9, 8 |
| IX | 5.8 | 3.1 | 63 | 3.0 | 1.4 | 49 | 18.2 | 10.2 | 61 | 8.2 | 5.1 | 67 | 6 |
| X | 7.2 | 5.2 | 69 | 3.5 | 2.2 | 66 | 23.5 | 16.5 | 71 | 9.0 | 6.5 | 72 | 8 |
| XI | 5.6 | 3.7 | 70 | 2.0 | 1.2 | 68 | 15.6 | 11.1 | 72 | 6.7 | 5.1 | 77 | 5, 8, 8, 6 |
| XII | 6.0 | 3.6 | 64 | 2.6 | 1.8 | 77 | 18.7 | 11.6 | 69 | 8.2 | 5.1 | 76 | 8, 8, 9, 8 |
| I(No.7) | 5.1 | 3.4 | 70 | 2.2 | 1.6 | 70 | 21.4 | 13.6 | 64 | 6.6 | 4.1 | 75 | 7, 7, 7, 6 |
| II | 5.0 | 3.2 | 64 | 1.8 | 1.5 | 84 | 16.1 | 9.8 | 62 | 5.9 | 4.2 | 70 | 8, 7, 8, 7 |
| III | 5.8 | 4.7 | 76 | 2.1 | 1.7 | 72 | 20.6 | 17.1 | 80 | 7.4 | 5.5 | 71 | 9 |
| IV | 5.5 | 3.0 | 59 | 3.0 | 1.7 | 57 | 19.4 | 11.0 | 58 | 8.6 | 5.0 | 60 | 10 |
| V | 9.5 | 6.4 | 70 | 4.2 | 2.6 | 62 | 34.6 | 22.1 | 66 | 13.1 | 8.8 | 63 | 16 |
| VI | 5.8 | 3.2 | 57 | 2.9 | 1.8 | 60 | 18.5 | 11.4 | 66 | 8.5 | 6.2 | 74 | 6 |
| VII | 10.4 | 5.5 | 58 | 3.7 | 2.3 | 67 | 31.7 | 18.5 | 63 | 12.1 | 7.8 | 69 | 6 |
| VIII | 7.5 | 5.0 | 67 | 3.0 | 2.0 | 69 | 27.0 | 17.0 | 59 | 9.0 | 6.0 | 70 | 4 |
| IX | 7.2 | 5.0 | 63 | 4.6 | 2.5 | 62 | 26.0 | 16.8 | 71 | 11.9 | 6.5 | 57 | 6, 5, 6, 6 |
| X | 8.3 | 6.3 | 74 | 3.8 | 2.4 | 62 | 26.8 | 17.2 | 69 | 11.4 | 7.9 | 70 | 13, 12, 13, 12 |
| XI | 7.9 | 5.1 | 71 | 2.9 | 1.8 | 72 | 23.3 | 16.4 | 76 | 9.3 | 6.4 | 71 | 9 |
| XII | 5.3 | 4.3 | 80 | 1.9 | 1.5 | 79 | 18.7 | 15.6 | 84 | 6.2 | 5.2 | 86 | 7, 8, 7, 8 |

Continued — table 1

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|----------|------|-----|----|-----|-----|----|------|------|----|------|------|----|----------------|----|
| I(No.8) | 9.2 | 5.1 | 65 | 2.8 | 1.8 | 72 | 19.8 | 13.0 | 74 | 7.3 | 4.7 | 70 | 4, 3, 4, 3 | |
| II | 7.6 | 4.9 | 59 | 3.3 | 2.3 | 64 | 27.1 | 17.4 | 58 | 11.3 | 7.6 | 64 | 9 | |
| III | 5.2 | 3.7 | 60 | 2.9 | 2.0 | 70 | 19.8 | 14.4 | 72 | 9.6 | 6.8 | 62 | 5 | |
| IV | 8.0 | 5.2 | 58 | 3.6 | 2.2 | 58 | 25.9 | 17.9 | 63 | 11.9 | 7.8 | 63 | 10 | |
| V | 8.1 | 4.0 | 60 | 3.6 | 2.3 | 69 | 25.6 | 13.9 | 64 | 10.6 | 7.2 | 67 | 9 | |
| VI | 5.4 | 3.5 | 64 | 2.5 | 1.8 | 77 | 14.8 | 10.5 | 72 | 8.0 | 5.5 | 65 | 4 | |
| VII | 5.8 | 3.7 | 62 | 2.8 | 2.0 | 69 | 17.0 | 11.4 | 68 | 8.6 | 6.0 | 67 | 6, 5, 5, 5 | |
| VIII | 6.1 | 3.0 | 54 | 2.2 | 1.6 | 71 | 16.2 | 9.0 | 57 | 7.0 | 5.0 | 70 | 4, 4, 5, 4 | |
| IX | 4.4 | 2.9 | 65 | 2.4 | 1.5 | 60 | 14.1 | 9.4 | 70 | 7.1 | 5.3 | 77 | 7, 8, 8, 8 | |
| X | 14.0 | 6.0 | 57 | 5.1 | 2.3 | 59 | 44.7 | 20.6 | 57 | 16.4 | 9.1 | 59 | 9, 9, 9, 8 | |
| XI | 9.4 | 5.4 | 69 | 4.1 | 1.9 | 58 | 27.6 | 15.1 | 64 | 14.4 | 7.2 | 62 | 4, 5, 5, 4 | |
| XII | 5.4 | 4.4 | 86 | 2.4 | 1.5 | 66 | 19.0 | 13.2 | 71 | 7.3 | 4.3 | 61 | 5 | |
| I(No.9) | 8.9 | 3.6 | 55 | 3.8 | 1.6 | 54 | 27.3 | 13.0 | 59 | 12.0 | 5.7 | 59 | 7, 6, 7, 7 | |
| II | 4.4 | 2.4 | 55 | 1.7 | 1.2 | 73 | 15.0 | 7.6 | 50 | 5.5 | 3.8 | 66 | 5 | |
| III | 6.9 | 4.6 | 65 | 3.5 | 2.1 | 62 | 21.4 | 13.8 | 63 | 9.4 | 5.6 | 58 | 7 | |
| IV | 10.6 | 6.6 | 67 | 4.1 | 2.8 | 71 | 36.2 | 25.0 | 71 | 14.8 | 14.1 | 72 | 9 | |
| V | 7.0 | 3.0 | 46 | 3.5 | 2.0 | 57 | 25.0 | 8.7 | 37 | 12.3 | 6.3 | 54 | 3 | |
| VI | 9.3 | 6.2 | 70 | 4.5 | 3.0 | 72 | 31.2 | 20.4 | 65 | 15.1 | 10.0 | 72 | 8 | |
| VII | 5.3 | 3.5 | 65 | 2.3 | 1.7 | 72 | 19.0 | 13.3 | 69 | 7.7 | 6.2 | 79 | 3 | |
| VIII | 4.9 | 3.4 | 57 | 2.8 | 1.7 | 64 | 20.4 | 12.6 | 66 | 8.6 | 5.5 | 67 | 8, 10, 9, 10 | |
| IX | 6.7 | 4.0 | 55 | 2.5 | 1.5 | 63 | 17.3 | 12.3 | 74 | 9.7 | 5.7 | 64 | 3 | |
| X | 6.4 | 4.1 | 64 | 3.4 | 2.1 | 63 | 22.7 | 14.9 | 66 | 11.0 | 7.0 | 66 | 16, 14, 16, 14 | |
| XI | 4.9 | 2.6 | 56 | 2.2 | 1.3 | 64 | 18.2 | 10.7 | 63 | 9.0 | 5.2 | 64 | 6 | |
| XII | 8.7 | 5.5 | 69 | 3.5 | 2.0 | 65 | 26.6 | 19.2 | 72 | 10.4 | 7.3 | 72 | 5 | |
| I(No.10) | 5.2 | 3.6 | 68 | 2.4 | 1.8 | 68 | 16.7 | 12.2 | 74 | 6.5 | 4.8 | 76 | 6 | |
| II | 11.0 | 5.3 | 51 | 4.8 | 2.6 | 59 | 32.2 | 18.8 | 59 | 13.5 | 7.8 | 60 | 3, 4, 4, 4 | |
| III | 7.4 | 3.4 | 61 | 2.9 | 1.9 | 65 | 28.5 | 11.5 | 54 | 8.5 | 5.2 | 64 | 4 | |
| IV | 13.8 | 7.2 | 50 | 3.9 | 2.6 | 65 | 45.8 | 23.2 | 49 | 13.0 | 8.6 | 66 | 5 | |
| V | 9.2 | 5.2 | 55 | 3.4 | 2.5 | 80 | 33.2 | 19.5 | 56 | 10.1 | 7.2 | 75 | 4 | |
| VI | 5.8 | 2.6 | 52 | 2.8 | 1.9 | 70 | 17.3 | 8.8 | 60 | 6.2 | 3.8 | 60 | 6 | |
| VII | 7.5 | 5.0 | 69 | 2.9 | 2.0 | 71 | 20.4 | 15.1 | 76 | 8.4 | 6.8 | 84 | 6, 7, 7, 7 | |
| VIII | 5.2 | 3.2 | 64 | 2.7 | 1.8 | 72 | 20.3 | 11.8 | 63 | 8.6 | 5.7 | 69 | 7 | |
| IX | 6.2 | 3.4 | 56 | 2.8 | 1.7 | 61 | 21.0 | 14.0 | 67 | 8.8 | 6.1 | 73 | 5 | |
| X | 7.9 | 4.8 | 69 | 4.1 | 2.3 | 62 | 27.6 | 16.6 | 69 | 13.5 | 7.9 | 4 | 13, 11, 14, 12 | |
| XI | 5.0 | 2.8 | 64 | 2.7 | 1.6 | 77 | 17.0 | 9.4 | 60 | 8.2 | 5.2 | 75 | 8, 7, 8, 8 | |
| XII | 7.6 | 4.8 | 63 | 2.7 | 1.7 | 67 | 21.9 | 12.9 | 58 | 8.6 | 5.4 | 68 | 6, 7, 7, 7 | |

Table 2

| Zones | D_1^0 | \bar{D}_2^0 | ${}^0sD_{12}$ | 0d_1 | 0d_2 | ${}^0s d_{12}$ | \bar{D}_3^0 | \bar{D}_4^0 | ${}^0sD_{34}$ | 0d_3 | 0d_4 | ${}^0s d_{34}$ | n_k |
|-------|---------|---------------|---------------|-----------|-----------|----------------|---------------|---------------|---------------|-----------|-----------|----------------|----------------|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| No. 1 | 6.4 | 5.4 | 806 | 2.7 | 2.2 | 828 | 26.9 | 21.6 | 810 | 9.5 | 7.7 | 822 | 25 |
| | 6.9 | 5.4 | 785 | 3.2 | 2.4 | 763 | 23.6 | 18.4 | 770 | 10.1 | 7.8 | 788 | 22, 21, 22, 22 |
| | 4.7 | 3.2 | 705 | 2.5 | 1.8 | 744 | 17.8 | 14.3 | 822 | 7.5 | 5.6 | 773 | 15, 16, 14, 16 |
| | 10.7 | 8.6 | 832 | 3.7 | 3.0 | 832 | 35.3 | 30.8 | 830 | 12.3 | 9.8 | 838 | 13, 14, 13, 14 |
| No. 2 | 7.3 | 5.7 | 778 | 3.1 | 2.3 | 816 | 25.0 | 19.4 | 796 | 9.7 | 7.3 | 802 | 24, 25, 26, 25 |
| | 5.3 | 3.5 | 721 | 2.4 | 1.9 | 831 | 19.3 | 12.4 | 699 | 8.0 | 6.3 | 824 | 31, 28, 31, 29 |
| | 6.5 | 4.4 | 694 | 3.2 | 2.3 | 711 | 22.4 | 17.0 | 760 | 10.5 | 7.4 | 733 | 23, 21, 23, 22 |
| No. 3 | 6.0 | 4.5 | 765 | 2.9 | 2.2 | 770 | 22.4 | 16.6 | 773 | 8.9 | 6.7 | 794 | 30, 29, 30, 30 |
| | 8.5 | 5.2 | 678 | 3.0 | 2.3 | 750 | 27.6 | 18.0 | 690 | 9.5 | 7.1 | 771 | 23, 21, 23, 21 |
| | 6.0 | 4.1 | 718 | 3.2 | 2.4 | 742 | 23.0 | 15.0 | 691 | 9.7 | 6.5 | 746 | 34, 33, 34, 34 |
| | 7.5 | 4.5 | 651 | 3.6 | 2.1 | 654 | 24.2 | 16.0 | 684 | 10.8 | 6.8 | 708 | 27, 28, 29, 27 |
| | 11.3 | 7.0 | 697 | 4.4 | 2.9 | 708 | 41.5 | 28.3 | 737 | 14.8 | 10.0 | 742 | 24 |

Continued — table 2

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|--------|------|-----|-----|-----|-----|-----|------|------|-----|------|-----|-----|----------------|
| No. 4 | 10.2 | 7.5 | 749 | 4.1 | 2.9 | 740 | 34.7 | 29.2 | 813 | 12.7 | 9.3 | 724 | 23, 21, 23, 22 |
| | 5.6 | 3.9 | 679 | 2.7 | 1.7 | 685 | 18.1 | 14.0 | 742 | 8.1 | 4.9 | 642 | 19, 19, 21, 19 |
| | 7.9 | 4.6 | 632 | 3.4 | 2.3 | 710 | 25.6 | 17.0 | 693 | 9.4 | 6.7 | 711 | 25, 25, 25, 24 |
| No. 5 | 7.2 | 4.9 | 723 | 3.1 | 2.4 | 763 | 25.0 | 18.4 | 758 | 10.1 | 7.8 | 800 | 21, 23, 23, 23 |
| | 9.0 | 5.2 | 599 | 3.7 | 2.4 | 680 | 29.4 | 20.1 | 675 | 11.7 | 7.9 | 702 | 20 |
| | 8.1 | 5.3 | 667 | 4.1 | 2.5 | 656 | 28.3 | 19.5 | 675 | 13.5 | 8.4 | 647 | 19, 18, 20, 18 |
| No. 6 | 8.8 | 4.5 | 588 | 3.4 | 2.2 | 706 | 25.0 | 15.0 | 666 | 9.9 | 6.3 | 688 | 25, 25, 26, 26 |
| | 8.0 | 4.6 | 615 | 4.0 | 2.4 | 621 | 29.5 | 16.6 | 595 | 12.1 | 7.2 | 637 | 24, 22, 24, 22 |
| | 7.6 | 5.1 | 676 | 3.3 | 2.3 | 692 | 24.4 | 17.9 | 724 | 10.7 | 7.2 | 692 | 20, 19, 20, 18 |
| No. 7 | 6.2 | 4.3 | 690 | 3.1 | 1.9 | 698 | 20.6 | 13.5 | 683 | 9.2 | 6.0 | 713 | 26, 24, 26, 24 |
| | 7.2 | 4.9 | 694 | 3.9 | 2.4 | 640 | 25.8 | 17.6 | 674 | 11.8 | 7.6 | 665 | 22 |
| | 8.6 | 5.5 | 641 | 3.7 | 2.6 | 690 | 29.1 | 19.4 | 674 | 11.7 | 7.8 | 698 | 18, 16, 18, 16 |
| No. 8 | 7.2 | 5.2 | 722 | 3.1 | 2.2 | 736 | 24.0 | 17.0 | 709 | 9.9 | 7.0 | 716 | 30, 28, 30, 28 |
| | 6.1 | 3.9 | 637 | 2.4 | 1.8 | 795 | 20.6 | 14.0 | 674 | 7.6 | 5.6 | 752 | 23, 24, 24, 24 |
| | 8.4 | 4.9 | 646 | 3.8 | 2.4 | 655 | 32.5 | 20.1 | 644 | 12.5 | 7.7 | 682 | 32, 32, 32, 31 |
| No. 9 | 5.9 | 4.1 | 745 | 2.8 | 1.8 | 656 | 19.5 | 13.7 | 729 | 8.6 | 5.9 | 691 | 19, 18, 20, 17 |
| | 9.6 | 5.1 | 625 | 4.1 | 2.0 | 589 | 33.4 | 17.1 | 612 | 12.5 | 6.5 | 626 | 20 |
| | 8.2 | 4.9 | 623 | 3.3 | 2.2 | 637 | 28.8 | 18.3 | 623 | 11.4 | 7.5 | 610 | 18, 16, 18, 16 |
| No. 10 | 8.0 | 4.7 | 583 | 3.5 | 2.3 | 638 | 31.3 | 18.4 | 567 | 11.5 | 7.4 | 606 | 23 |
| | 5.8 | 3.9 | 615 | 3.0 | 1.8 | 617 | 20.6 | 13.4 | 667 | 7.8 | 5.5 | 724 | 16, 18, 17, 18 |
| | 7.5 | 5.2 | 685 | 3.2 | 2.3 | 678 | 27.4 | 18.3 | 671 | 10.6 | 7.4 | 700 | 28, 27, 29, 27 |
| No. 10 | 7.5 | 4.0 | 582 | 3.4 | 2.1 | 721 | 27.5 | 15.7 | 619 | 10.6 | 6.2 | 672 | 19 |
| | 10.9 | 6.6 | 627 | 4.5 | 2.9 | 669 | 37.7 | 27.2 | 706 | 14.8 | 9.6 | 678 | 20 |
| | 6.9 | 4.5 | 693 | 3.1 | 2.2 | 699 | 23.8 | 16.5 | 718 | 10.0 | 6.6 | 684 | 19, 19, 17, 19 |
| No. 10 | 7.4 | 4.2 | 652 | 3.3 | 1.8 | 640 | 25.5 | 15.1 | 641 | 10.9 | 6.1 | 660 | 30, 29, 31, 28 |
| | 7.5 | 5.0 | 696 | 3.3 | 2.0 | 690 | 26.2 | 16.6 | 681 | 10.0 | 6.4 | 683 | 15 |
| | 9.4 | 5.5 | 600 | 3.3 | 2.3 | 741 | 29.7 | 18.6 | 667 | 10.8 | 7.0 | 735 | 18, 17, 18, 17 |

| | \overline{D}_1^E | \overline{D}_2^E | $\frac{-E}{s_{012}}$ | $\frac{-E}{d_1}$ | $\frac{-E}{d_2}$ | $\frac{-E}{s_{d_{12}}}$ | \overline{D}_3^E | \overline{D}_4^E | $\frac{-E}{s_{D_{31}}}$ | $\frac{-E}{d_3}$ | $\frac{-E}{d_4}$ | $\frac{-E}{s_{d_{31}}}$ | n_k |
|-------|--------------------|--------------------|----------------------|------------------|------------------|-------------------------|--------------------|--------------------|-------------------------|------------------|------------------|-------------------------|----------------|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| No. 1 | 8.9 | 7.3 | 807 | 2.8 | 2.3 | 817 | 29.0 | 24.4 | 835 | 9.3 | 7.9 | 863 | 18, 26, 21, 26 |
| | 7.9 | 5.9 | 762 | 3.4 | 2.6 | 815 | 23.7 | 19.3 | 813 | 10.8 | 8.4 | 819 | 18, 20, 20, 20 |
| | 4.5 | 3.1 | 725 | 2.3 | 1.8 | 795 | 18.2 | 13.9 | 801 | 7.5 | 5.6 | 762 | 12, 14, 10, 15 |
| No. 2 | 9.6 | 7.6 | 855 | 3.7 | 2.9 | 877 | 32.5 | 27.2 | 881 | 12.5 | 10.2 | 845 | 13, 15, 14, 15 |
| | 7.0 | 5.6 | 853 | 3.1 | 2.4 | 802 | 22.8 | 18.5 | 827 | 9.9 | 7.5 | 838 | 22, 24, 25, 24 |
| | 5.0 | 3.3 | 734 | 2.3 | 1.9 | 847 | 16.7 | 11.3 | 736 | 7.1 | 5.8 | 842 | 28, 30, 31, 31 |
| No. 3 | 6.0 | 4.1 | 702 | 3.0 | 2.1 | 713 | 19.4 | 14.5 | 739 | 10.5 | 7.1 | 737 | 24, 23, 24, 21 |
| | 6.4 | 4.2 | 736 | 2.9 | 2.1 | 749 | 21.6 | 15.9 | 775 | 9.8 | 7.5 | 794 | 25, 24, 26, 23 |
| | 6.1 | 3.9 | 743 | 2.9 | 2.0 | 825 | 20.6 | 13.7 | 731 | 19.9 | 6.5 | 754 | 32, 33, 33, 32 |
| No. 4 | 7.8 | 5.0 | 666 | 3.0 | 2.1 | 727 | 25.5 | 17.3 | 671 | 9.8 | 7.1 | 769 | 21, 20, 22, 20 |
| | 6.9 | 4.3 | 685 | 3.5 | 2.2 | 723 | 23.3 | 14.4 | 665 | 10.7 | 7.1 | 741 | 27, 27, 28, 27 |
| | 9.6 | 6.2 | 697 | 4.6 | 3.0 | 760 | 35.1 | 22.4 | 720 | 15.1 | 9.6 | 705 | 24 |
| No. 5 | 6.6 | 4.7 | 731 | 2.8 | 2.2 | 801 | 23.2 | 16.6 | 708 | 9.1 | 6.9 | 765 | 21, 22, 22, 22 |
| | 6.6 | 4.3 | 705 | 2.9 | 1.8 | 637 | 22.7 | 14.3 | 687 | 8.8 | 5.6 | 669 | 24, 25, 25, 25 |
| | 9.1 | 6.4 | 716 | 3.8 | 2.7 | 751 | 29.7 | 23.3 | 750 | 13.5 | 9.7 | 734 | 23, 21, 23, 21 |
| No. 6 | 7.4 | 4.4 | 645 | 3.5 | 2.2 | 656 | 24.5 | 14.8 | 621 | 12.0 | 7.2 | 628 | 24, 23, 24, 21 |
| | 7.6 | 4.1 | 620 | 3.0 | 1.7 | 628 | 23.0 | 13.1 | 636 | 9.3 | 5.9 | 700 | 24, 24, 25, 24 |
| | 8.3 | 5.1 | 618 | 3.8 | 2.3 | 646 | 26.0 | 17.8 | 687 | 11.9 | 8.7 | 676 | 19, 20, 20, 20 |
| No. 6 | 6.7 | 4.4 | 670 | 3.4 | 2.2 | 663 | 23.6 | 16.3 | 680 | 10.0 | 7.0 | 697 | 22 |
| | 6.1 | 3.5 | 594 | 2.9 | 1.7 | 598 | 21.5 | 12.4 | 593 | 9.4 | 5.8 | 633 | 22, 20, 22, 19 |
| | 7.2 | 4.7 | 639 | 3.1 | 2.1 | 669 | 24.4 | 17.4 | 698 | 9.8 | 6.9 | 712 | 19, 18, 18, 18 |
| No. 6 | 6.4 | 4.2 | 671 | 2.7 | 1.8 | 704 | 19.2 | 13.0 | 706 | 8.1 | 5.6 | 750 | 21, 24, 25, 22 |
| | 7.5 | 4.8 | 640 | 3.6 | 2.2 | 602 | 26.8 | 16.6 | 636 | 10.8 | 7.1 | 644 | 32 |
| | 5.3 | 3.8 | 704 | 2.0 | 1.6 | 751 | 19.3 | 13.6 | 696 | 6.7 | 4.9 | 752 | 24, 23, 24, 22 |

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | |
|-------|------|-----|-----|-----|-----|-----|------|------|-----|------|------|-----|----------------|----------------|
| No. 7 | 8.5 | 5.2 | 620 | 3.8 | 2.3 | 657 | 28.4 | 17.5 | 649 | 11.3 | 6.8 | 645 | 16, 15, 16, 16 | |
| | 7.5 | 5.4 | 746 | 3.0 | 1.9 | 697 | 23.8 | 16.6 | 752 | 9.3 | 6.7 | 747 | | 29 |
| | 7.5 | 4.4 | 597 | 3.5 | 2.2 | 659 | 23.8 | 15.0 | 651 | 10.7 | 7.2 | 650 | | 23 |
| No. 8 | 7.3 | 4.6 | 608 | 3.1 | 2.1 | 673 | 23.4 | 15.6 | 657 | 10.1 | 6.9 | 646 | 18, 17, 18, 17 | |
| | 5.3 | 3.2 | 616 | 2.5 | 1.7 | 654 | 17.4 | 11.1 | 656 | 7.5 | 5.4 | 726 | | 17, 17, 18, 17 |
| | 10.6 | 5.4 | 678 | 4.1 | 2.0 | 606 | 33.4 | 17.2 | 622 | 13.3 | 7.3 | 602 | | 18, 19, 19, 17 |
| No. 9 | 9.5 | 5.9 | 652 | 4.2 | 2.8 | 697 | 32.6 | 20.7 | 645 | 14.6 | 11.3 | 694 | 20 | |
| | 7.0 | 3.7 | 585 | 3.1 | 1.7 | 623 | 21.9 | 11.9 | 582 | 9.3 | 5.2 | 604 | | 19, 18, 19, 19 |
| | 6.5 | 4.0 | 630 | 3.2 | 1.9 | 635 | 22.4 | 14.8 | 665 | 10.4 | 6.7 | 664 | | 27, 25, 27, 25 |
| No. 9 | 5.4 | 3.6 | 582 | 2.6 | 1.7 | 653 | 19.5 | 12.7 | 681 | 8.6 | 5.7 | 685 | 14, 16, 15, 16 | |
| | 9.4 | 4.8 | 522 | 3.3 | 2.3 | 711 | 31.1 | 16.5 | 555 | 9.5 | 6.3 | 662 | | 15 |
| | 7.2 | 3.9 | 622 | 3.2 | 2.0 | 645 | 24.5 | 13.9 | 639 | 9.1 | 5.8 | 679 | | 13, 14, 14, 14 |

axies and their nuclei. Let us denote the above mentioned characteristics as follows:

$$\begin{array}{cc}
 D_1^O & \varepsilon_{D_{12}}^O \\
 D_2^O & \\
 d_1^O & \varepsilon_{d_{12}}^O \\
 d_2^O & \\
 D_3^O & \varepsilon_{D_{24}}^O \\
 D_4^O & \\
 d_3^O & \varepsilon_{d_{24}}^O \\
 d_4^O &
 \end{array}
 \quad
 \begin{array}{cc}
 D_1^E & \varepsilon_{D_{12}}^E \\
 D_2^E & \\
 d_1^E & \varepsilon_{d_{12}}^E \\
 d_2^E & \\
 D_3^E & \varepsilon_{D_{24}}^E \\
 D_4^E & \\
 d_3^E & \varepsilon_{d_{24}}^E \\
 d_4^E &
 \end{array}$$

The indices O and E are reserved for both prints, 1 and 2 — for major and minor diameters measured with $16\times$, 3 and 4 — for major and minor diameters with $56\times$. The diameters of the outer parts of the galaxies are labelled with D , and those of the nuclei with d . The ratios of the minor diameters to the major ones give the quantities $\varepsilon = D_2/D_1$; d_2/d_1 .

All average characteristics (with respect to n — the number of galaxies measured) are given on Table 1. The numbers of the measured galaxies are given on the right side of the Table and represent each group of 3 characteristics, since in some cases the nuclei or the outer parts of the galaxies either do not exist or cannot be measured.

Errors in all characteristics will be discussed in the following paper. The D_1 , D_2 and d_2 values (O and E) have small errors. For example when $1 < D$; $d < 25$ the mean-root-square error is of about 0.3 divisions. It is clear that the error depends on the type of the galaxies measured. This question is examined by Vorontsov-Velyaminov [23], Agekian and Soomsina [24] and discussed in [25].

In order to avoid the defects in Vorontsov-Velyaminov's method, dimensions of outer parts of the galaxies were determined up to an almost blend-

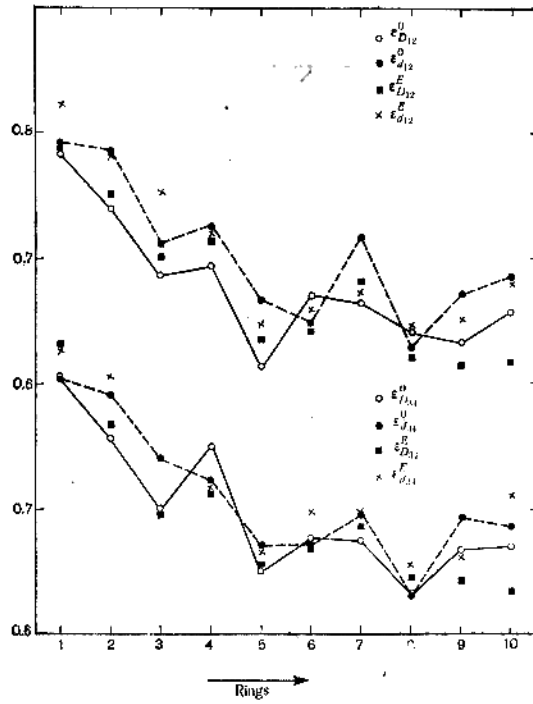


Fig. 1

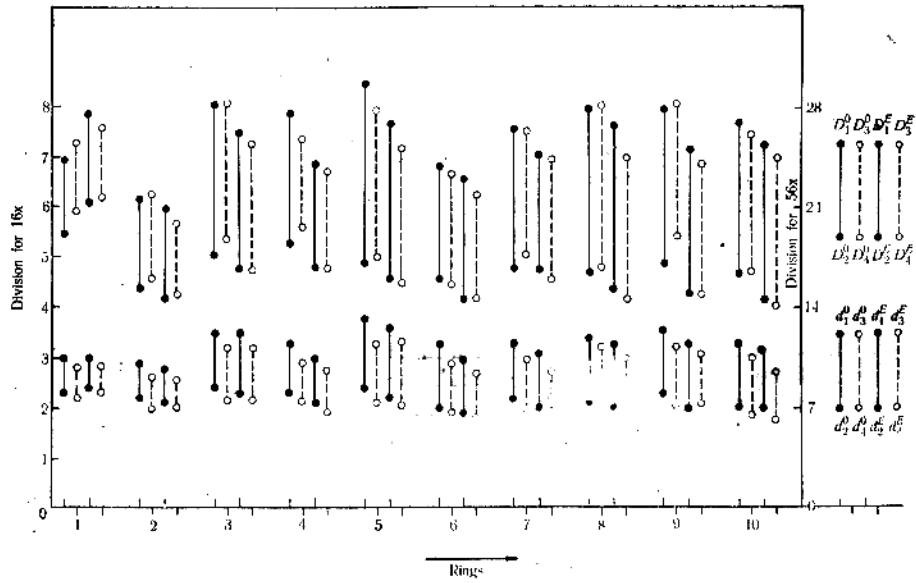


Fig. 2

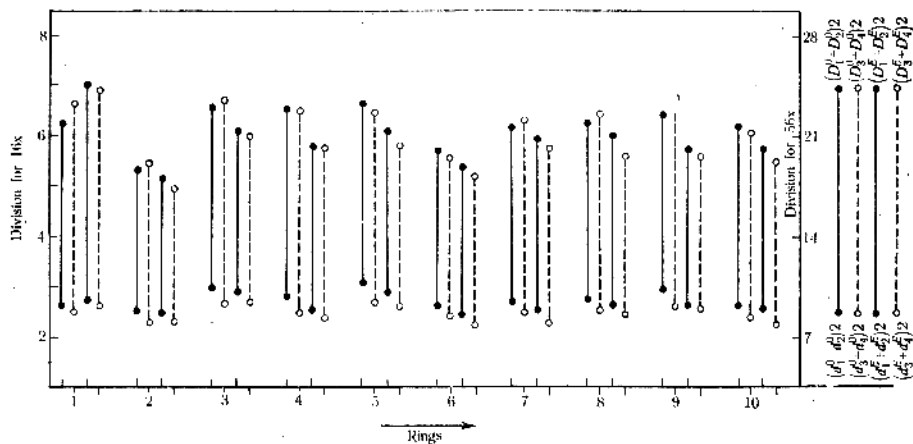


Fig. 3

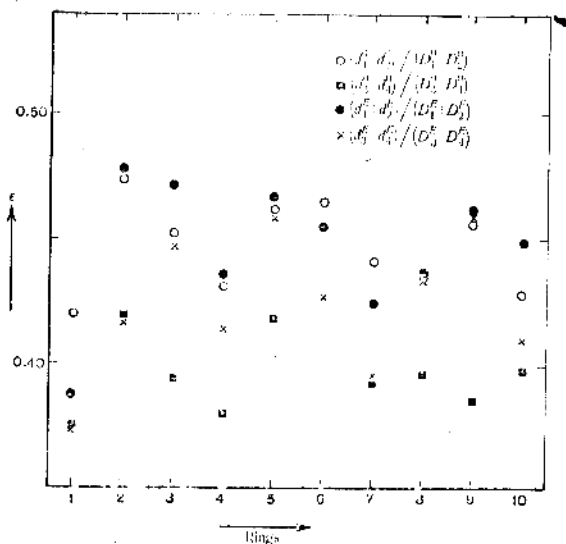


Fig. 4

ing into the background. The dimensions of the nuclei were determined from the greatest gradient of blackening (which gives a large uncertainty for elliptical galaxies)

The values of ε are in connection with the type of the galaxies (for elliptical systems only) according to Hubble, since $\varepsilon = D_2/D_1$; $e = 10 \cdot (D_1 - D_2)/D_1 = 10(1 - D_2/D_1) = 10(1 - \varepsilon)$.

The Table 1 data are necessary for a study of the Coma cluster microstructures, but for macrostructures one needs results, which are obtained as a weighted average from the above mentioned values.

Table 2 presents data for z Zones which are grouped in 3 sectors for given radial distances from the center (No 1—3, 4—6, 7—9, 10—12 — four quadrants). The radial variations of all characteristics related to the ten rings are given on Fig. 1 — for ε , Fig. 2 — for diameters of outer parts and nuclei of the galaxies and on Fig. 3 — for the mean diameters. The radial variations of ratios between the mean diameters of nuclei and outer parts are shown on Fig. 4.

The above mentioned results give the following important quality information about the Coma cluster structure:

1. The values of ε_d are larger than those of ε_D — Tables 1 and 2 and mostly — Fig. 1. Consequently, the nuclei of the galaxies possesses a smaller flattening than the outer parts of the galaxies.

2. The radial variation of ε (for all cases) show that in the central part of the Coma cluster there are galaxies with a smaller flattening — real spheroidal systems. This fact is connected to the dynamical stability of the cluster, as well as to its rotation.

COUNTS OF GALAXIES

Numerous attempts have been made to investigate the surface distribution of galaxies in the Coma cluster — as in large investigations (i. e. Lick counts [8, 9]) and also in special ones [1, 2, 5] and others.

In the present paper a count of galaxies is made too. The basic material is given on Table 3 — by means of sectors and rings. All counts are obtained with a 16 \times magnifications. As it may be seen an effect exists according to which the counts on the E print are larger than the counts on the O print, since for larger radial distances from the cluster center it is more probable to indicate the faintest background galaxies (as a result of the reddening for larger z).

Table 3

| Sector <i>O</i> | Rings | | | | | | | | | | Sector <i>E</i> | Rings | | | | | | | | |
|--------------------|-------|----|----|----|----|----|----|----|----|----|--------------------|-------|----|----|----|----|----|----|----|----|
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| I | 5 | 12 | 12 | 14 | 17 | 18 | 12 | 15 | 11 | 16 | 5 | 15 | 10 | 15 | 16 | 21 | 15 | 20 | 15 | 15 |
| II | 11 | 11 | 11 | 15 | 12 | 10 | 11 | 10 | 11 | 16 | 10 | 13 | 17 | 16 | 13 | 9 | 13 | 13 | 12 | 20 |
| III | 15 | 12 | 11 | 12 | 15 | 8 | 18 | 12 | 14 | 10 | 15 | 13 | 12 | 9 | 13 | 7 | 16 | 12 | 13 | 9 |
| IV | 11 | 13 | 29 | 16 | 15 | 12 | 14 | 26 | 20 | 14 | 10 | 13 | 27 | 18 | 18 | 13 | 15 | 28 | 18 | 15 |
| V | 8 | 12 | 23 | 10 | 10 | 13 | 23 | 20 | 11 | 7 | 9 | 12 | 18 | 8 | 8 | 14 | 19 | 18 | 12 | 9 |
| VI | 9 | 20 | 7 | 9 | 9 | 7 | 10 | 15 | 16 | 10 | 8 | 15 | 7 | 11 | 9 | 7 | 15 | 19 | 16 | 9 |
| VII | 7 | 13 | 18 | 10 | 11 | 7 | 13 | 12 | 10 | 11 | 8 | 14 | 17 | 8 | 10 | 7 | 11 | 12 | 12 | 12 |
| VIII | 2 | 11 | 9 | 11 | 10 | 12 | 5 | 9 | 13 | 14 | 2 | 8 | 11 | 9 | 10 | 11 | 6 | 8 | 13 | 18 |
| IX | 8 | 12 | 15 | 15 | 12 | 18 | 11 | 14 | 15 | 11 | 8 | 13 | 15 | 15 | 13 | 19 | 13 | 13 | 15 | 13 |
| X | 8 | 13 | 18 | 11 | 11 | 17 | 16 | 21 | 27 | 22 | 8 | 13 | 17 | 9 | 14 | 14 | 19 | 21 | 26 | 22 |
| XI | 4 | 15 | 9 | 10 | 13 | 17 | 16 | 18 | 11 | 15 | 5 | 16 | 10 | 12 | 17 | 14 | 18 | 16 | 15 | 17 |
| XII | 5 | 8 | 9 | 12 | 10 | 15 | 11 | 15 | 15 | 17 | 4 | 9 | 10 | 12 | 9 | 17 | 14 | 22 | 18 | 22 |

The function $\lg N(m)$ for all radial sectors, reduced to 1 sq. degree are given on Fig. 5, together with the results from [2] and [5]. Our count is in compliance with these results.

A more complete picture of the galaxy's surface distribution in direction to the Coma cluster is presented on Fig. 6 and Fig. 7, where the values of $\lg N(m)$ are given for the separate zones.

The observational material gives a possibility to study in detail the surface distribution of the galaxies. For this purpose it is necessary to construct the curves of radial surface densities — Fig. 8 and Fig. 9. The separate values, plotted on the latter two Figures, are obtained as a moving arith-

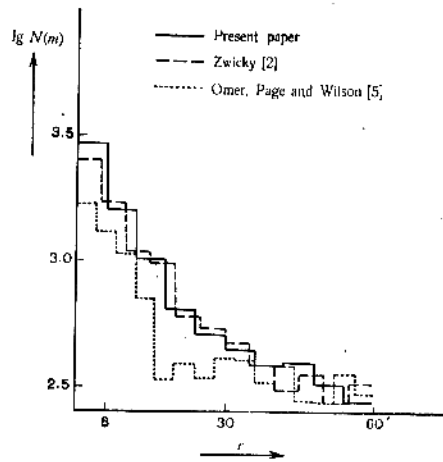


Fig. 5

metic mean from 4 neighbouring surface densities. After this method polar diagrams may be constructed — Fig. 10 and Fig. 11.

Let us suppose that the polar diagrams may be approximated with ellipses. Let us choose the origin of the co-ordinate system in the cluster center and let the directions of the axes X and Y be N and E , respectively. a and b are the major and minor semiaxes of the approximated ellipses, ψ — the polar angle of the major semiaxis a and φ — the polar angle of the radius-vector.

The equation of an ellipse in the polar co-ordinate system will be

$$(3) \quad \frac{1}{r^2} = \alpha + \beta \sin 2\psi + \gamma \cos 2\psi.$$

We have $n=12$ sectors, which permit the determination of the coefficients α , β and γ after the least-mean-square method

$$(4) \quad \begin{aligned} \alpha &= \frac{1}{12} \sum_{i=1}^{12} \frac{1}{r_i^2}, \\ \beta &= \frac{1}{6} \sum_{i=1}^{12} \frac{\sin 2\psi_i}{r_i^2}, \\ \gamma &= \frac{1}{6} \sum_{i=1}^{12} \frac{\cos 2\psi_i}{r_i^2}. \end{aligned}$$

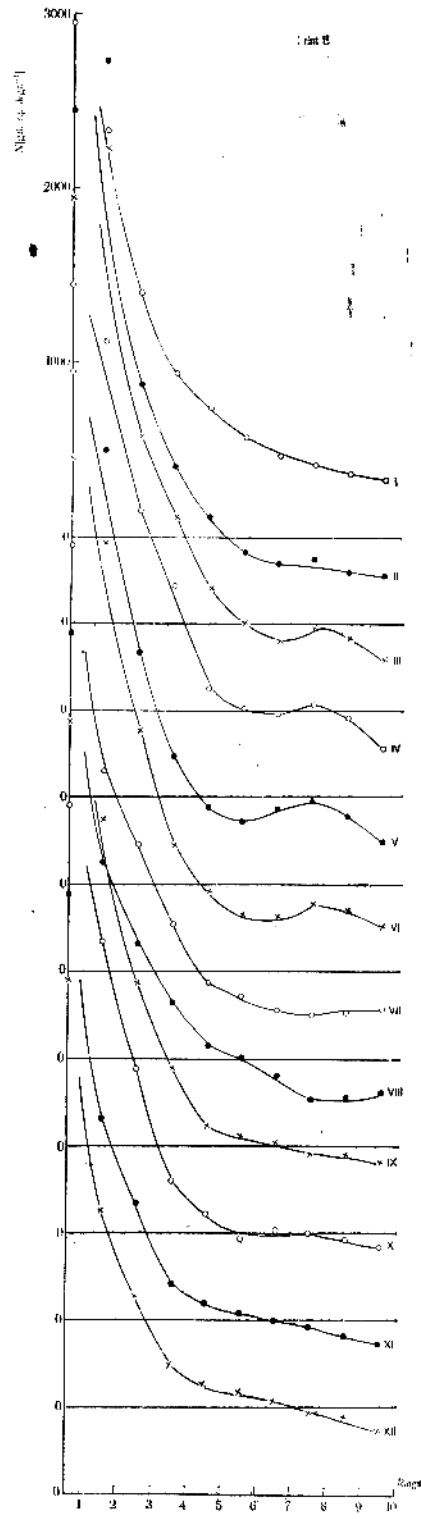
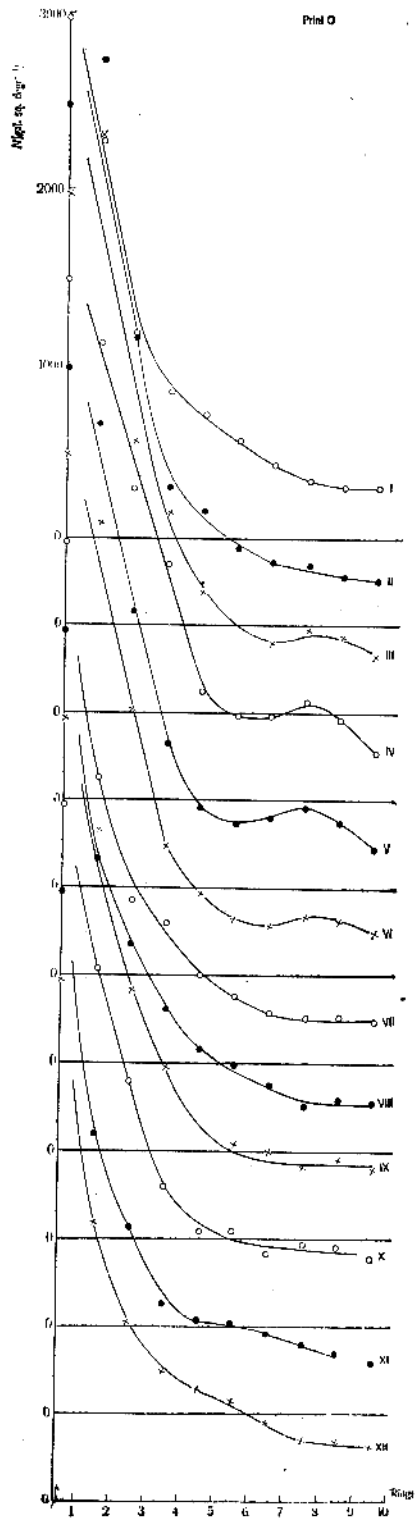


Fig. 8
Fig. 9

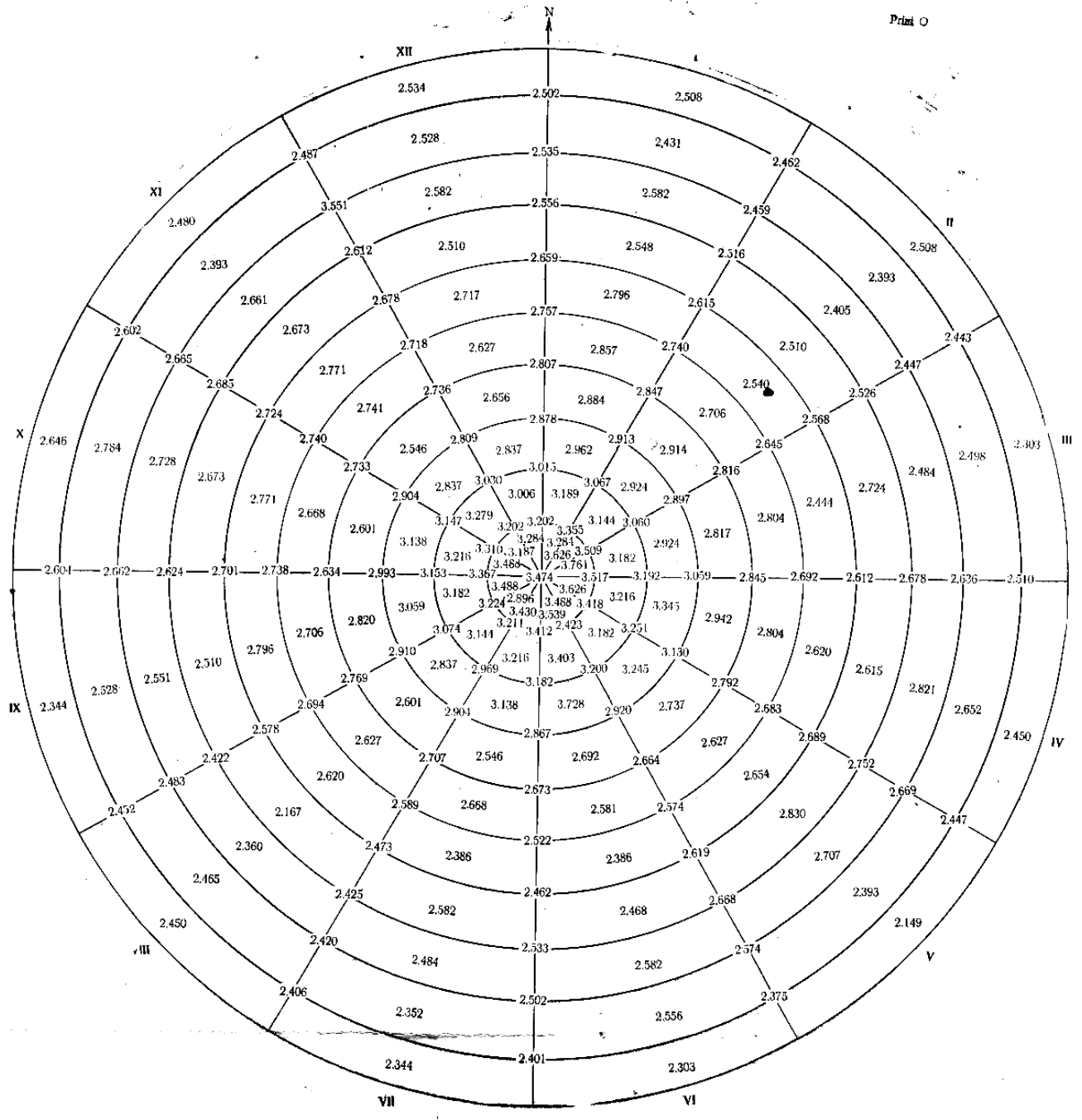


Fig. 6

M. Kalinkov - Investigation of the Coma cluster of galaxies
Известия на Седмичият по астрономия, т. IV

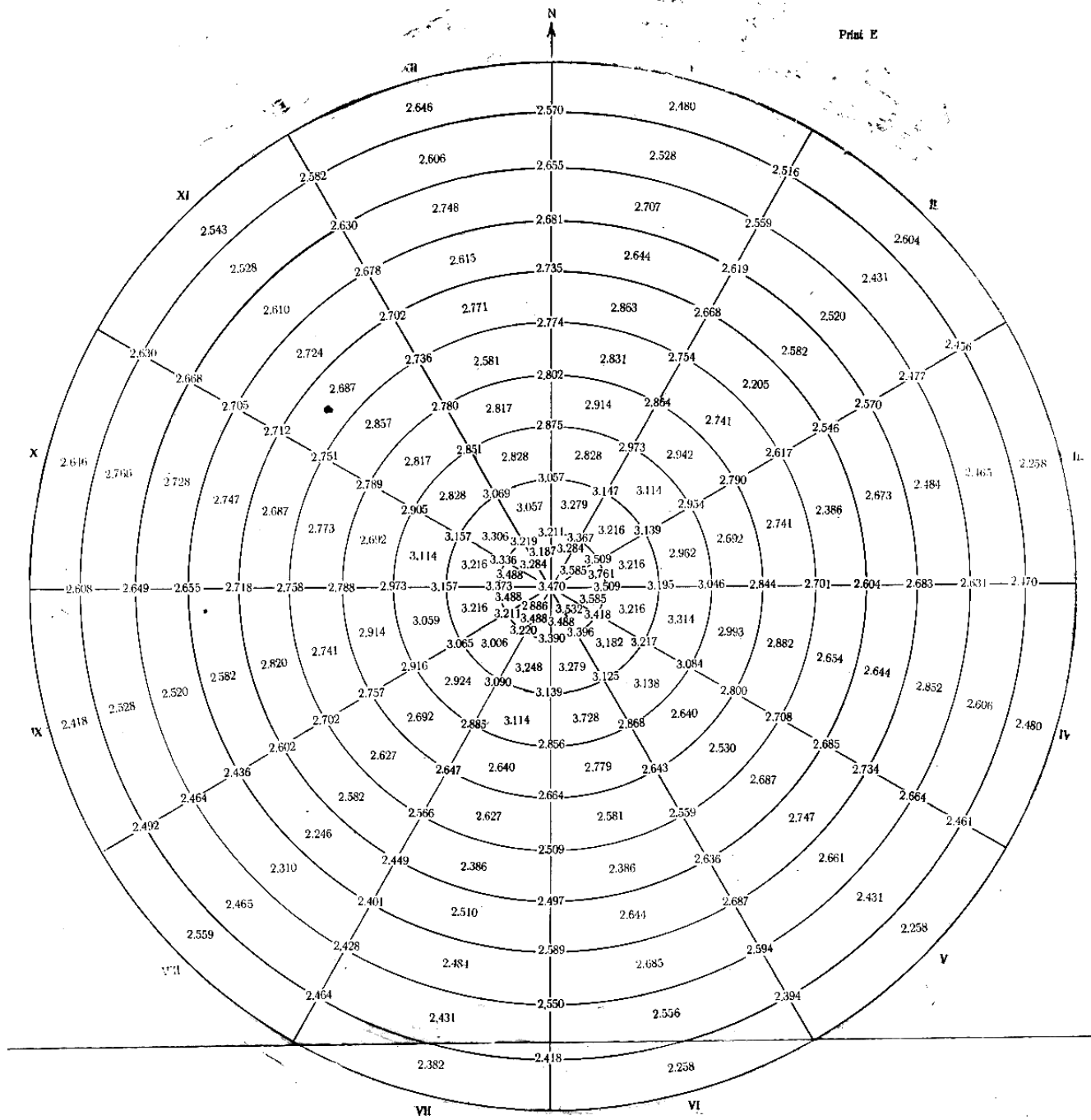


Fig. 7

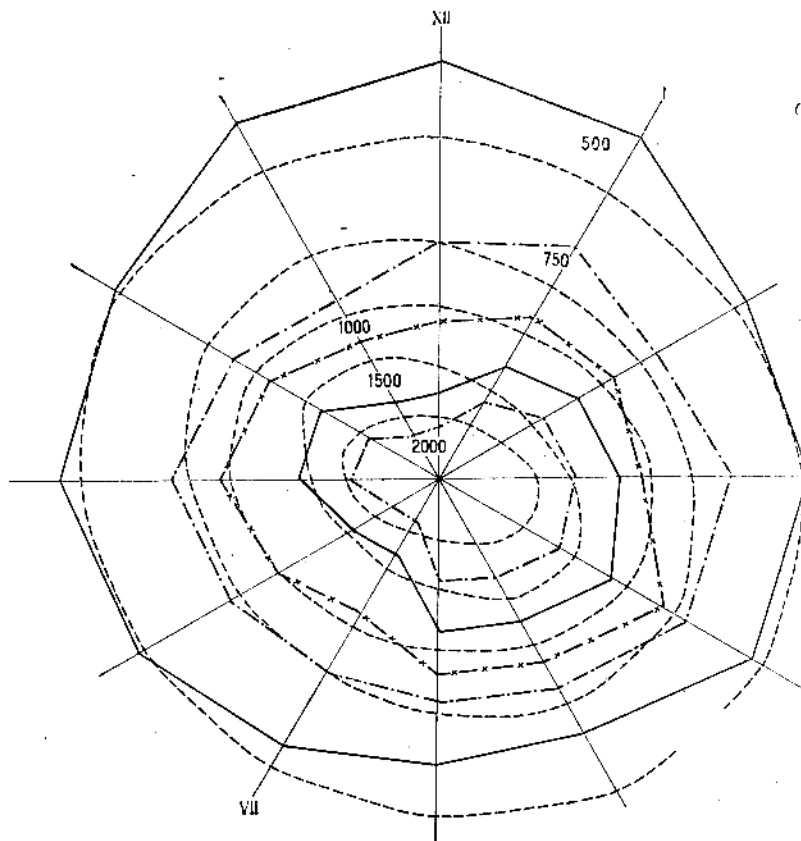


Fig. 10

with root-mean-square errors

$$(5) \quad \Delta\alpha = \left[\frac{\sum \left(\frac{1}{r_{i, \text{obs}}^2} - \frac{1}{r_{i, \text{calc}}^2} \right)^2}{n(n-3)} \right]^{1/2},$$

$$\Delta\beta = \Delta\gamma = \Delta\alpha \sqrt{2}$$

and

$$(6) \quad \text{tg } 2\varphi = \frac{\beta}{\gamma}$$

with

$$\Delta\varphi = \Delta\alpha [2(\beta^2 + \gamma^2)]^{-1/2}$$

and

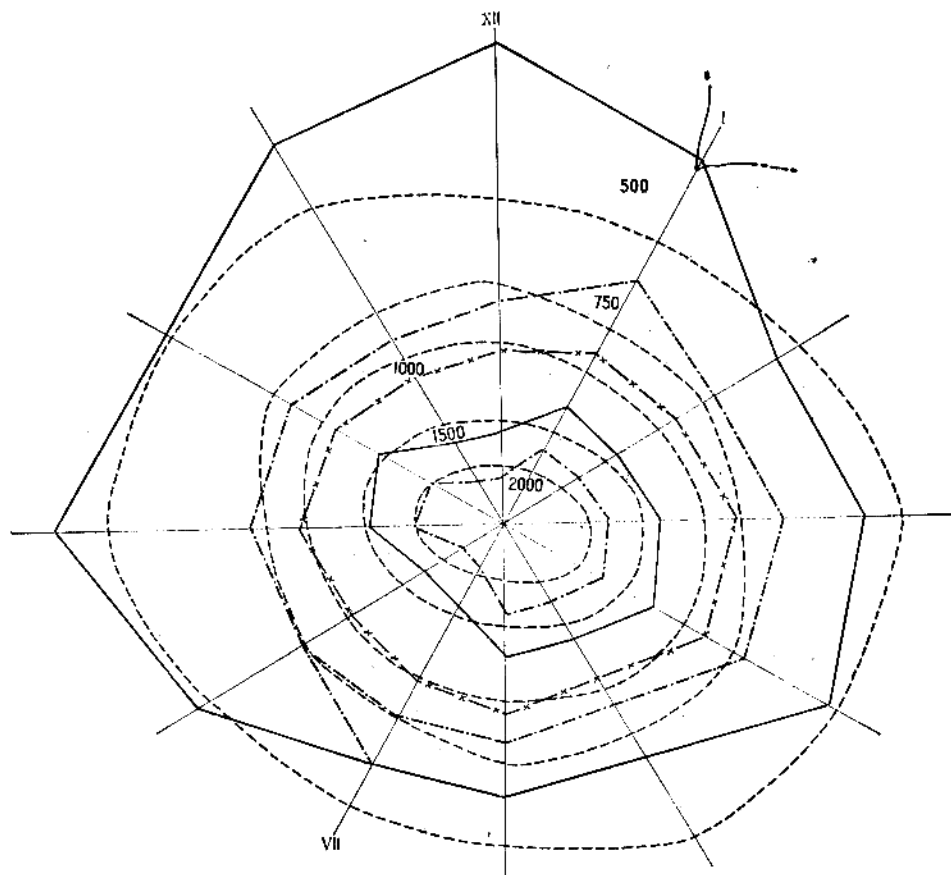


Fig. 11

$$(7) \quad \eta = \frac{b}{a} = \left[\frac{a - (\beta^2 + \gamma^2)^{1/2}}{a + (\beta^2 + \gamma^2)^{1/2}} \right]^{1/2}$$

with

$$(8) \quad \Delta\eta = \frac{1}{2} a^2 \eta \Delta\alpha (3 + 2\eta^2 + 3\eta^4)^{1/2}$$

according to [26, 27].

The application of the least-mean-square method for apparent surface densities 2 000, 1 500, 1 000, 750 and 500 gal/sq. degr. permits the determination of the following approximated ellipses present on Fig. 10 and Fig. 11 (r_i is in units of mm, as 20 mm correspond to 6 minutes of arc; P is the positional angle of the minor axes — is this the position angle of the cluster rotation axis? — in direction NESW):

$$O, 2\,000: \frac{1}{r_i^2} = 0.0026\,3557 - 0.0006\,8158 \cdot \sin 2\psi_i + 0.0010\,6091 \cdot \cos 2\psi_i$$

$$\pm 5\,7293 \quad \pm 8\,1012 \quad \pm 8\,1012$$

$$\eta = 0.594 \pm 0.250; \quad \varphi = 74^\circ \pm 18^\circ; \quad P = 344^\circ.$$

$$E, 2\,000: \frac{1}{r_i^2} = 0.0028\,8207 - 0.0007\,2352 \cdot \sin 2\psi_i - 0.0010\,4720 \cdot \cos 2\psi_i$$

$$\pm 5\,5300 \quad \pm 7\,8207 \quad \pm 7\,8207$$

$$\eta = 0.622 \pm 0.215; \quad \varphi = 72^\circ \pm 18^\circ; \quad P = 343^\circ.$$

$$O, 1\,500: \frac{1}{r_i^2} = 0.0009\,6621 - 0.0001\,8127 \cdot \sin 2\psi_i + 0.0003\,9183 \cdot \cos 2\psi_i$$

$$\pm 1\,5680 \quad \pm 2\,2172 \quad \pm 2\,2172$$

$$\eta = 0.618 \pm 0.186; \quad \varphi = 78^\circ \pm 15^\circ; \quad P = 347^\circ.$$

$$E, 1\,500: \frac{1}{r_i^2} = 0.0009\,6201 - 0.0001\,8801 \cdot \sin 2\psi_i + 0.0002\,5810 \cdot \cos 2\psi_i$$

$$\pm 1\,3438 \quad \pm 1\,9005 \quad \pm 1\,9005$$

$$\eta = 0.708 \pm 0.162; \quad \varphi = 72^\circ \pm 17^\circ; \quad P = 342^\circ.$$

$$O, 1\,000: \frac{1}{r_i^2} = 0.0003\,9072 - 0.0004\,1000 \cdot \sin 2\psi_i + 0.0000\,9192 \cdot \cos 2\psi_i$$

$$\pm 2712 \quad \pm 3836 \quad \pm 3836$$

$$\eta = 0.768 \pm 0.082; \quad \varphi = 78^\circ \pm 11^\circ; \quad P = 347^\circ.$$

$$E, 1\,000: \frac{1}{r_i^2} = 0.0003\,6316 - 0.0000\,0963 \cdot \sin 2\psi_i + 0.0000\,6641 \cdot \cos 2\psi_i$$

$$\pm 1597 \quad \pm 2258 \quad \pm 2258$$

$$\eta = 0.688 \pm 0.040; \quad \varphi = 86^\circ \pm 10^\circ; \quad P = 356^\circ.$$

$$O, 750: \frac{1}{r_i^2} = 0.0002\,3312 + 0.0000\,0724 \cdot \sin 2\psi_i + 0.0000\,4183 \cdot \cos 2\psi_i$$

$$\pm 1091 \quad \pm 1543 \quad \pm 1543$$

$$\eta = 0.692 \pm 0.043; \quad \varphi = 95^\circ \pm 10^\circ; \quad P = 5^\circ.$$

$$E, 750: \frac{1}{r_i^2} = 0.0002\,3280 + 0.0000\,0961 \cdot \sin 2\psi_i + 0.0000\,4368 \cdot \cos 2\psi_i$$

$$\pm 1044 \quad \pm 1476 \quad \pm 1476$$

$$\eta = 0.823 \pm 0.055; \quad \varphi = 96^\circ \pm 9^\circ; \quad P = 6^\circ.$$

$$O, 500: \frac{1}{r_i^2} = 0.0001\,1320 - 0.0000\,0134 \cdot \sin 2\psi_i + 0.0000\,1257 \cdot \cos 2\psi_i$$

$$\pm 917 \quad \pm 1296 \quad \pm 1296$$

$$\eta = 0.894 \pm 0.104; \quad \varphi = 87^\circ \pm 29^\circ; \quad P = 357^\circ.$$

$$E, 500: \frac{1}{r_i^2} = 0.0001\,0939 \pm 1367 - 0.0000\,0856 \pm 1933 \cdot \sin 2\psi_i + 0.0000\,1894 \pm 1933 \cdot \cos 2\psi_i$$

$$\eta = 0.825 \pm 0.153; \quad \varphi = 78^\circ \pm 27^\circ; \quad P = 348^\circ.$$

In [10, 11] an attempt for the determination of the Coma cluster of galaxies rotation was made. There are two possible hypotheses for the direction of the rotational axis. The present count permits a rejection of the first hypothesis for reasons, which are independent of those in [10, 11] — the basic results are obtained there by means of an analysis of the radial velocities. The determined position of the axis according to the previous paper (sector 1-2 — 7-8, or $P=330^\circ$) must be corrected, since the mean value of P here is $=348^\circ$ (as we exclude the counts for 750 gal./sq. degr.), i. e. the axis is located in sector 1.

Note. In a following paper [28] a comparison will be made among the diameters in the Coma cluster of galaxies according to several sources [12, 19, 20, 29, 30, 31].

The author expresses his gratitude to acad. V. Ambartsumian for his critical remarks and to Dr. J. Delhaye, Dr. E. Blum and Dr. J. Heidman from the Meudon Observatory (France) for permitting him to calculate serial models on IBM 7044/7096 and for the discussions. The author is also grateful to Prof. W. Zonn and Dr. K. Rudnicky (Warsaw, Poland, where some results are reported) for the numerous stimulating discussions.

The author would like to express his appreciation to Miss J. Kostova (Astronomical Section) for her generous assistance.

REFERENCES

1. Zwicky F., *Hand. Phys.*, **53**, 407, 1957.
2. Zwicky F., *Morphological Astronomy*, Berlin, 1957.
3. Abell G. O., in "Problems of Extra-Galactic Research", ed. by G. C. McVittie, N. Y., **213**, 1962.
4. Stebbins J. and A. E. Whitford, *Ap.J.*, **115**, 284, 1952.
5. Omer G. C., Th. Page and A. G. Wilson, *AJ*, **70**, 440, 1965.
6. Abell G. O., *Ap. J., Suppl. Ser.*, **3**, 211, 1958.
7. Abell G. O., *Ann. Rev. Astr. and Astrophys.*, **3**, 1, 1965.
8. Shane C. D., *Vistas in Astronomy*, **2**, 157, 1954.
9. Shane C. D. and C. A. Wirtanen, *A.J.*, **59**, 285, 1954.
10. Kalinkov M., *Astron. Circ. No. 475*, 4, 1968.
11. Kalinkov M., *CR l'Academy bulg. Sc.*, **621**, 1968.
12. Zwicky F. and coll, *Catalogue of Galaxies and Clusters of Galaxies*, Pasadena, 1961—1967.
13. Sharov A. S., *Ap.J.(Russian)*, **36**, 307, 1959.
14. Noonan T., *PASP*, **73**, 212, 1961.
15. Wallenquist A., *Arkiv för Astronomy*, **2**, 103, 1957.
16. Veleva B. and M. Kalinkov, *Bull. Sect. Astron.*, **2**, 151, 1967.
17. Kalinkov M. and B. Veleva (to be published).
18. Kalinkov M. (to be published).
19. Vorontsov-Velyaminov B. A. and V. P. Archipova, *Morfological Catalogue of Galaxies*, II, 1964.
20. Vaucouleurs G. de and A. de Vaucouleurs, *Reference Catalogue of Bright Galaxies*, Austine, 1964.

21. Kalinkov M. and N. Cholakova (to be published).
22. Karachentzev I. (private communication).
23. Vorontsov-Velyaminov B. A. and A. A. Krasnogorzskaja, Morphological Catalogue of Galaxies.
24. Agekjan T. and N. Soomsina, Astrophys'ca (Erevan).
25. Problems of Extra-Galactic Research, Ed. by G. C. McVittie, N. Y., 1962.
26. Idelson N. I., The least-mean-squares method, M., 1967.
27. Cholopov P. N., Contribution of GAI Sh, **23**, 250, 1953.
28. Kalinkov M. and B. Veleva, Unpublished.
29. Rood H. J. and W. A. Baum, Ap. J., **72**, 398, 1967.
30. Rood H. and W. A. Baum, Ap. J., **73**, 442, 1968.
31. Rood H. and B. E. Turnrose, Ap. J., **152**, 1057, 1968.

23. IX. 1968

ИССЛЕДОВАНИЕ СКОПЛЕНИЯ ГАЛАКТИК СОМА

М. Калинин

(Резюме)

Сделано исследование вращения скопления галактик Сомы при использовании измерений и подсчета галактик по Паломарскому атласу.

Важнейшие выводы следующие:

1. Ядра галактик этого скопления имеют меньшее сжатие, чем сами галактики.
2. В центральной части скопления расположены галактики с меньшим сжатием — сфероидальные системы.