

# The multiplicity fraction in 202 open clusters from *Gaia*

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**MW-GAIA WG2 Workshop – Stellar Variability, Stellar Multiplicity:  
Periodicity in Time & Motion**

Sofia (Bulgaria)

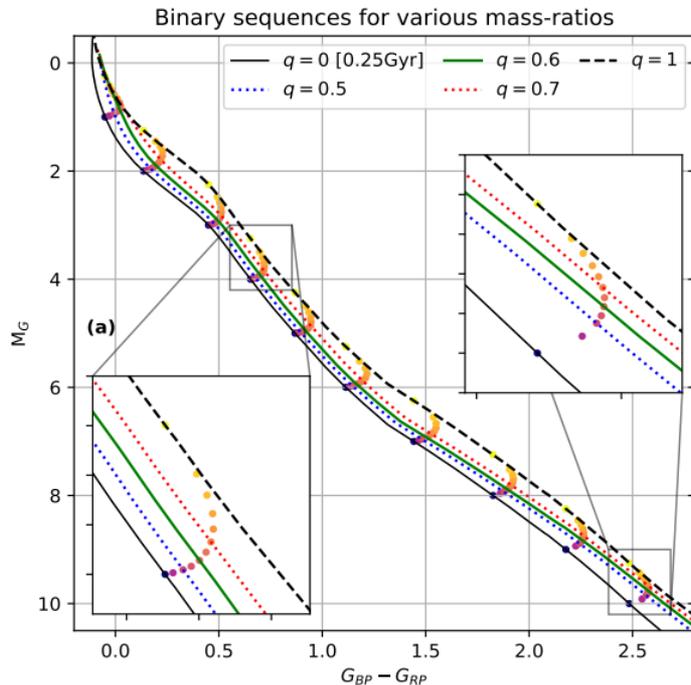
7<sup>th</sup> June 2023

Multiplicity fraction:  $f_b = \frac{B + T + \dots}{S + B + T + \dots}$

Binary system mass ratio:  $q = M_2/M_1$  ( $0 < q \leq 1$ )

### Multiple stellar systems in open clusters (OCs)

Most multiple systems are spatially unresolved, being located in the colour-magnitude diagram (CMD) above (and towards redder colours for  $q < 1$ ) with respect to the main-sequence position of the primary component, by an amount which depends on  $q$  and  $M_1$ .



- $q = 0$  locus: single-star sequence
- - -  $q = 1$  locus: equal-mass binary sequence (0.753 mag brighter than the equivalent single star)

Jadhav, Vikrant V. et al., *High Mass-Ratio Binary Population in Open Clusters: Segregation of Early Type Binaries and an Increasing Binary Fraction with Mass, 2021, AJ, 162.6, p. 264.*

# Selection of the sample of OCs and their main-sequence members

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## OCs' membership lists

Membership determinations of OCs in the extended solar neighbourhood (**closer than 1.5 kpc** from the Sun) from the *Gaia*-derived catalogues:

- **Tarricq et al. 2022 (T22, EDR3-based)**, age > 50 Myr

Tarricq, Y. et al., *Structural parameters of 389 local open clusters*, **2022**, *A&A*, 659, A59. arXiv: 2111.05291.

- **Cantat-Gaudin et al. 2020 (CGa20, DR2-based)**, selecting those of age < 50 Myr

Cantat-Gaudin, T. et al., *Painting a portrait of the Galactic disc with its stellar clusters*, **2020**, *A&A*, 640, A1. arXiv: 2004.07274.

Both are limited to  $G < 18$ , we further select those members with membership probability  $\geq 70\%$ .

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**OC's physical parameters:** from CGa20.

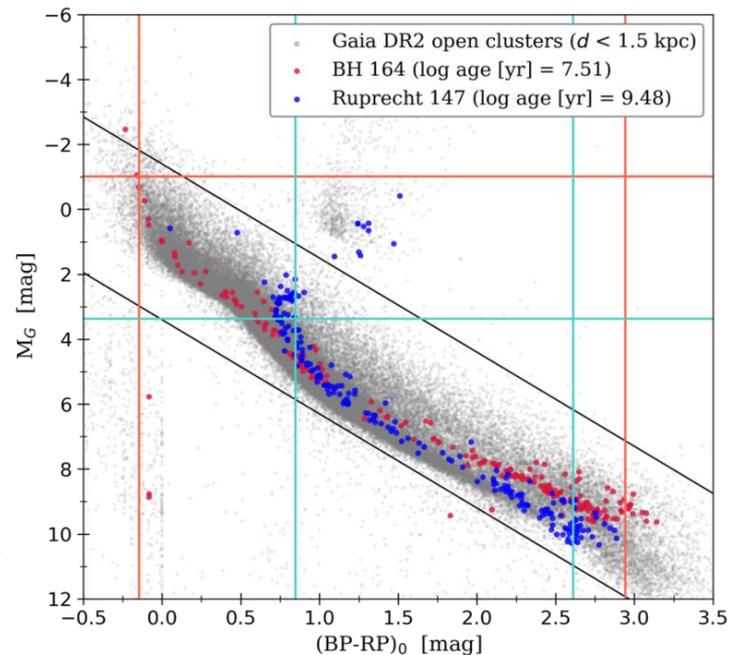
## Selection of OC's main-sequence (MS) members

We retain only those OCs having:

- at least 30 MS members
- $(BP - RP)_0$  range of at least 1 mag

and obtain 377 OCs.

Two examples of the homogeneous selection of the main sequence members of the OCs.



# Mixture model for the observed OC's *Gaia* CMD

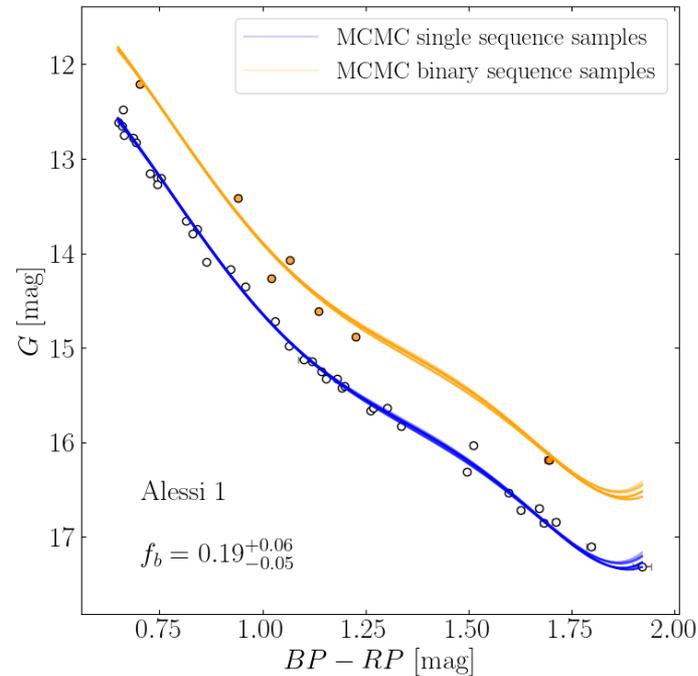
The observed  $G$  vs.  $(BP-RP)$  *Gaia* CMD of selected MS members is modelled as a mixture distribution

of  $\left\{ \begin{array}{l} \text{single stars} \\ \text{unresolved binaries} \end{array} \right.$  arising from 2 Gaussian distributions:  $\left\{ \begin{array}{l} \mathcal{N}(G; G_{SS}(M_1), \sigma_{SS}) \quad (\text{weight: } w_{SS}) \\ \mathcal{N}(G; G_{BS}(M_1), \sigma_{BS}) \quad (\text{weight: } w_{BS}) \end{array} \right.$

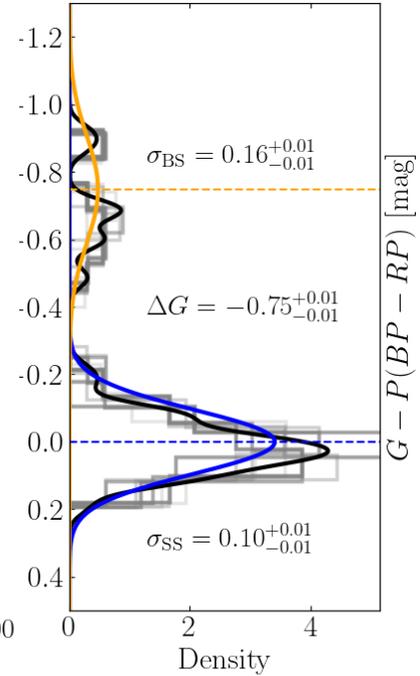
Likelihood function ( $\mathcal{L}$ ) depending on:

- $p+1$  parameters of  $p_{SS}$  polynomial ( $p=6$ )
- $\Delta G = G_{BS} - G_{SS}$
- $\sigma_{SS}$  (SS comprises  $q \in [0, q_{\text{lim}}(M_1)]$ )
- $\sigma_{BS}$  (BS comprises  $q \in (q_{\text{lim}}(M_1), 1]$ )
- $f_b(q > q_{\text{lim}}) = \frac{w_{BS}}{w_{SS} + w_{BS}} = w_{BS}$

**Multiplicity fraction of high- $q$  unresolved systems** integrated over the OC's MS mass range.



Fit of the single sequence ridge and the binary sequence in the observed *Gaia* CMD.



Residuals with respect to the polynomial fit and Gaussian mixture fit.

emcee is used for the MCMC sampling of the posterior probability distribution.

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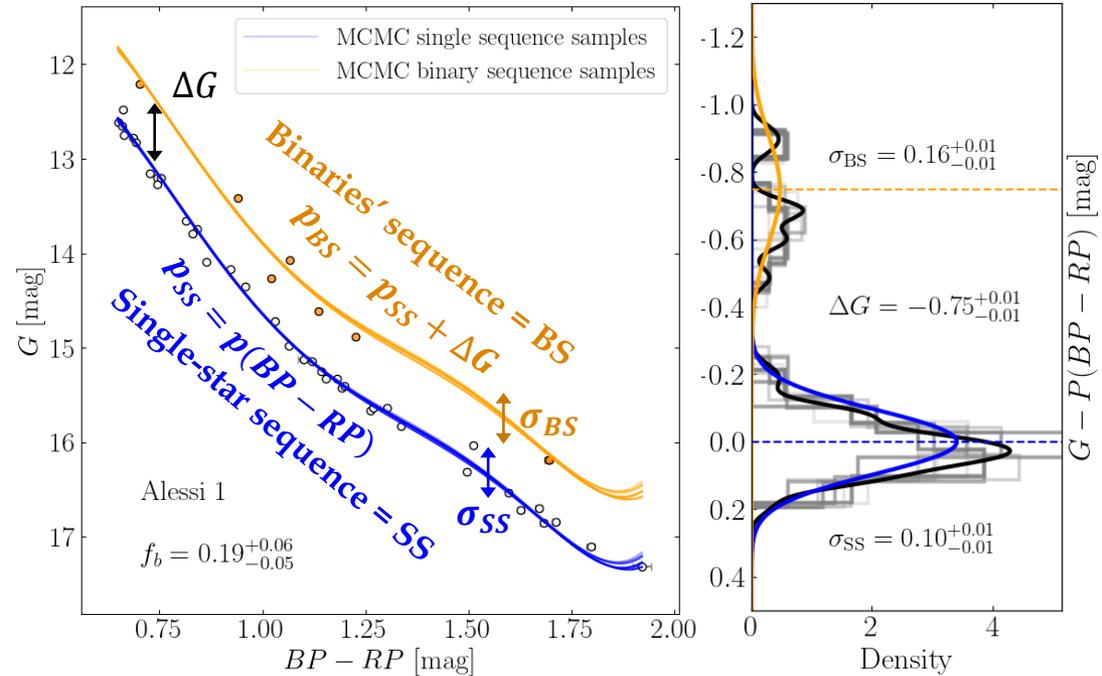
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Fit of the single sequence ridge and the binary sequence in the observed *Gaia* CMD.

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# Selection of OCs with an accurate CMD fit

We only retain the OCs having:

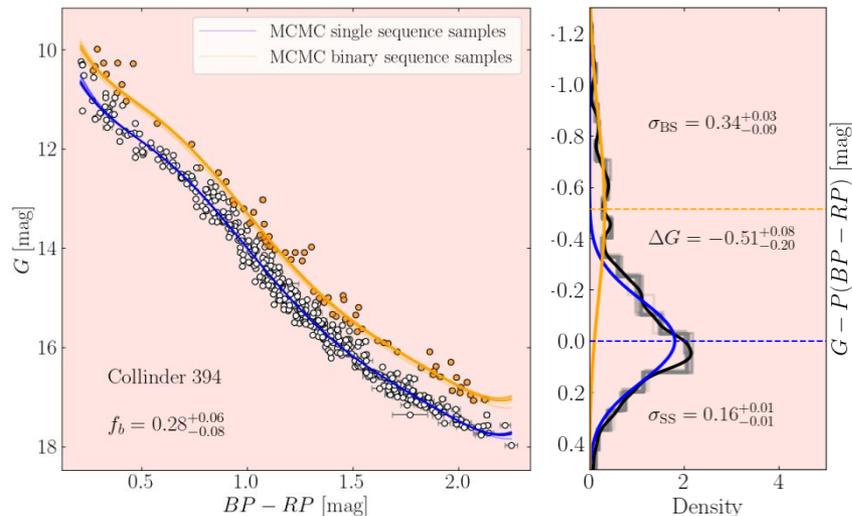
1.  $\sigma_{SS} \leq 0.2$
2.  $\sigma_{BS} \leq 0.25$
3.  $|\Delta G + 0.75| \leq 0.05$
4.  $\sigma_{f_b} \leq 0.25$
5. Well-fit CMD (visual inspection)

We obtain a final sample of **202 OCs**:

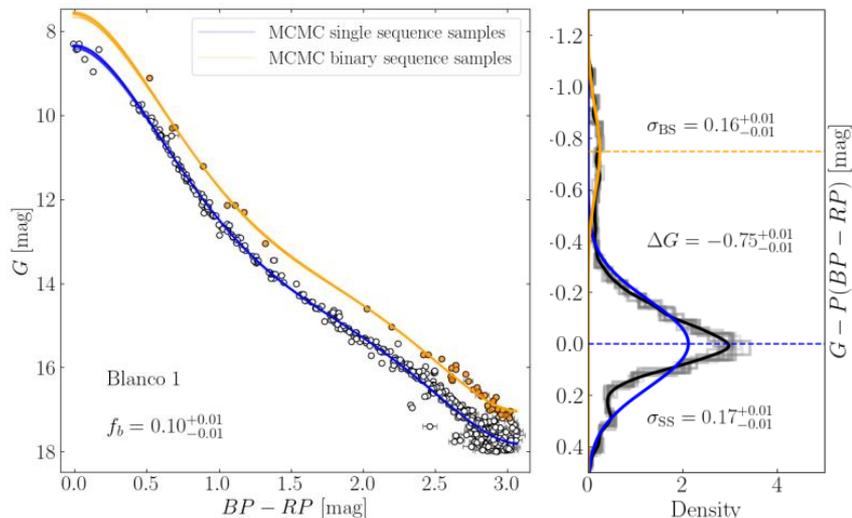
146 from T22 ( $\sim 72\%$ )

56 from CGa20 ( $\sim 28\%$ )

Example of a discarded OC:



Examples of selected OCs:

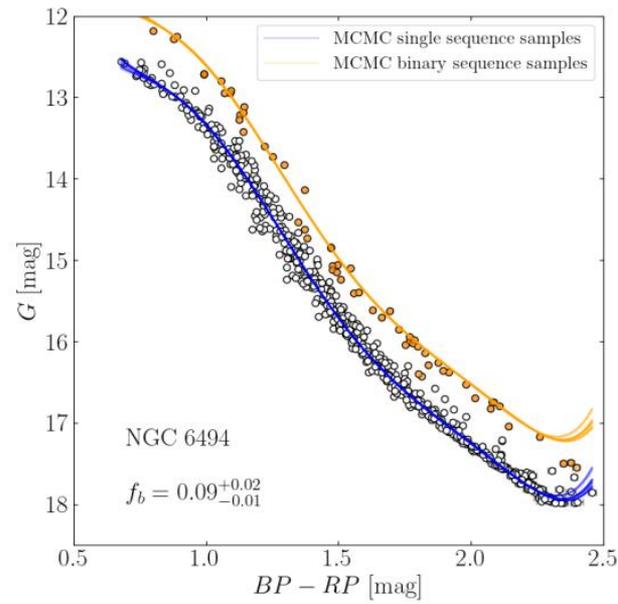
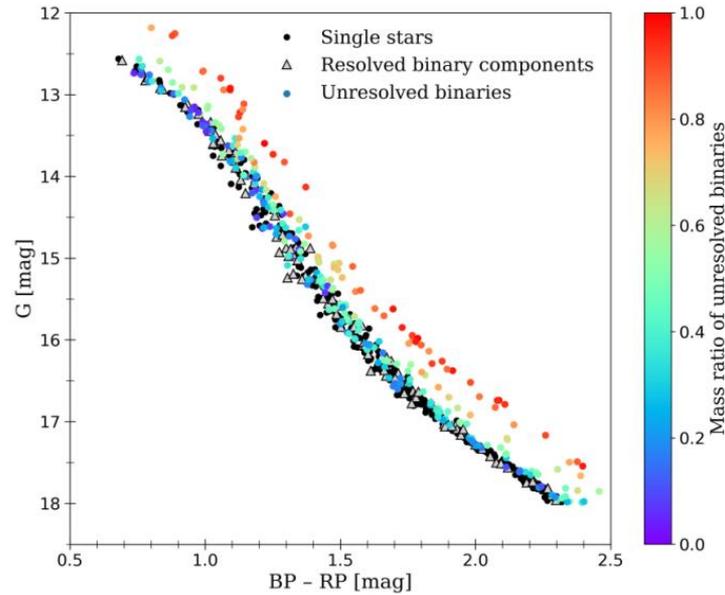


# Simulated *Gaia*-like OCs

Gaia Object Generator (GOG;  
Luri, X., et al. 2014, A&A, 566, A119)



Multiple-star module (Arenou, F. 2011, in American Institute of Physics Conference Series, Vol. 1346, 107–121) of the Gaia Universe Model simulations (Robin, A. C., et al. 2012, A&A, 543, A100)

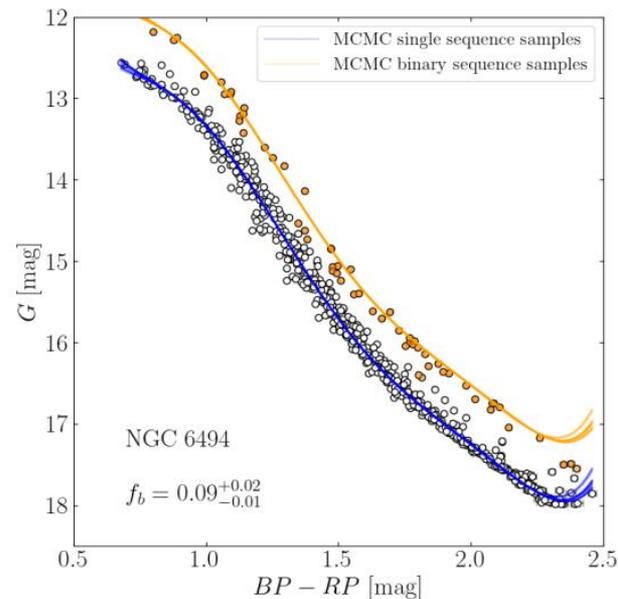
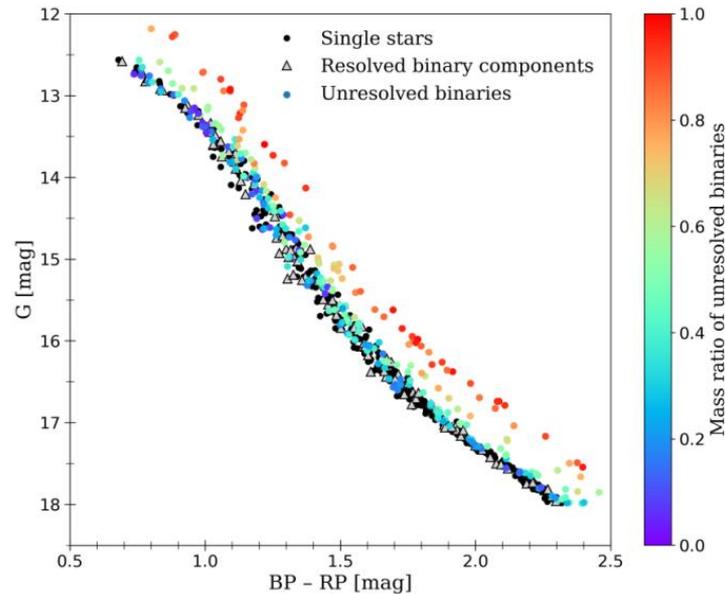


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A sample of **219 simulated OCs**, and **10 different CMD realisations each**, is used to:

- 1) Estimate the  $q_{\text{lim}}$  which the unresolved multiplicity fraction  $f_b(q > q_{\text{lim}})$  takes into account

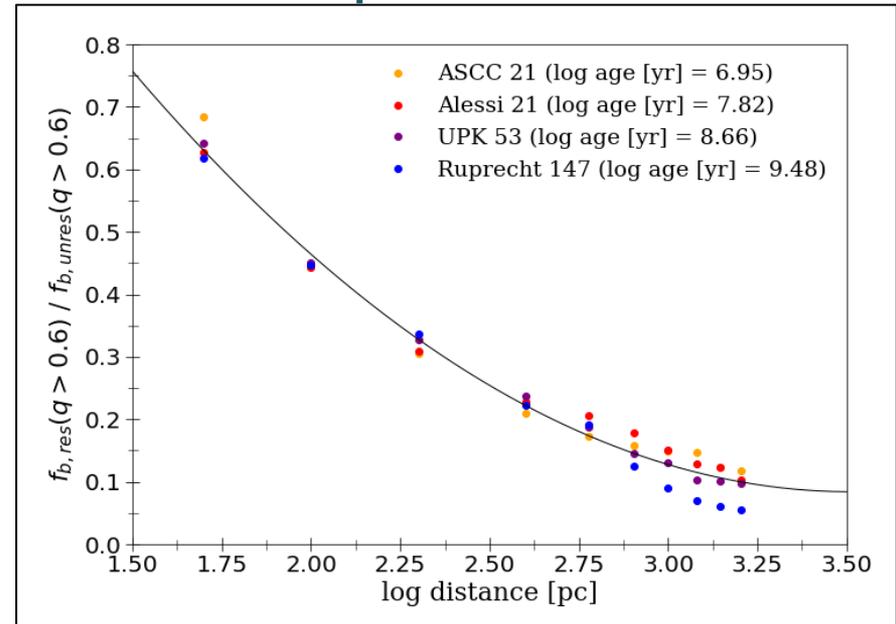
$q_{\text{lim}}$  is assumed to be the  $q_{\text{min}}$  for which  $\underbrace{\overline{f_b^{\text{sim, theo}}(q > q_{\text{min}})}}_{q_{\text{min}} \in [0.2, 0.7] \text{ in steps of } 0.05}$  is the closest possible to  $\underbrace{\overline{f_b^{\text{sim}}}}_{\text{from MCMC fit to the CMD}}$

We find:  $q_{\text{lim}} = 0.6^{+0.05}_{-0.15}$

# Simulated *Gaia*-like OCs

2) Use simulated OCs to estimate the OC's **total multiplicity fraction**

$$f_b^{tot}(q > q_{lim} = 0.6_{-0.15}^{+0.05}) = \underbrace{f_{b,unres}^{MCMC}(q > q_{lim})}_{\text{From MCMC fit in the observed } Gaia \text{ CMD}} \cdot \left[ 1 + \underbrace{\frac{f_{b,res}^{sim,theo}(q > q_{lim}; d)}{f_{b,unres}^{sim,theo}(q > q_{lim}; d)}}_{\text{Estimated through a fit as a function of the OC's distance}} \right]$$



## Results and discussion

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**Homogeneous catalogue** accessible via CDS containing the estimated **unresolved and total multiplicity fractions** of main-sequence systems of  $q > 0.6_{-0.15}^{+0.05}$  for 202 OCs closer than 1.5 kpc, having ages between 6.6 Myr and 3.0 Gyr.

$f_b \in [5, 67]\%$ , median: 15%.

$f_b^{tot} \in [6, 80]\%$ , median: 18%. For 89% of the OCs,  $f_b^{tot} - f_b < 5\%$ .

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## 1) Comparison to other studies

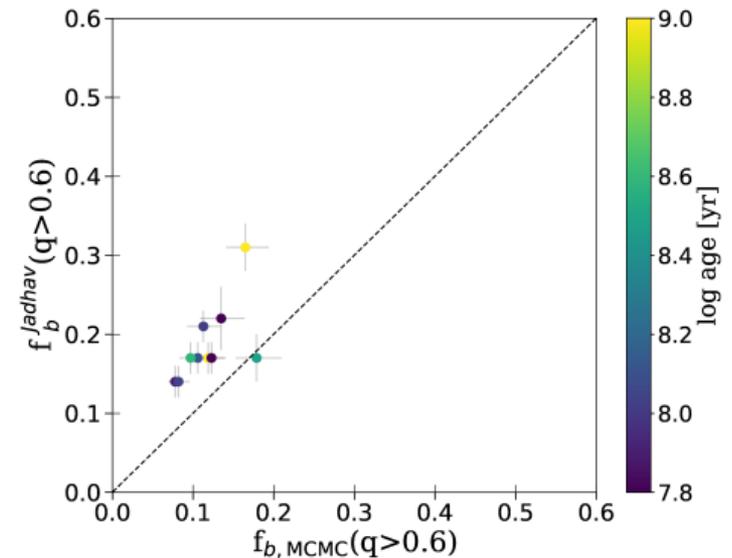
Large homogeneous studies are still rare.

Results of different studies are very seldom directly comparable:

- Different mass range of the OC is covered
- Different  $q_{lim}$
- Dependence on the applied model's assumptions
- Different OC membership determinations

Recent studies of multiplicity fraction in OCs:

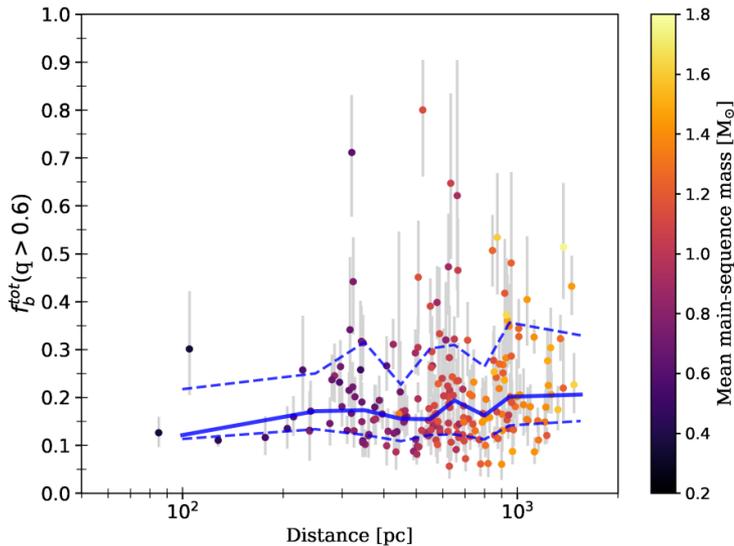
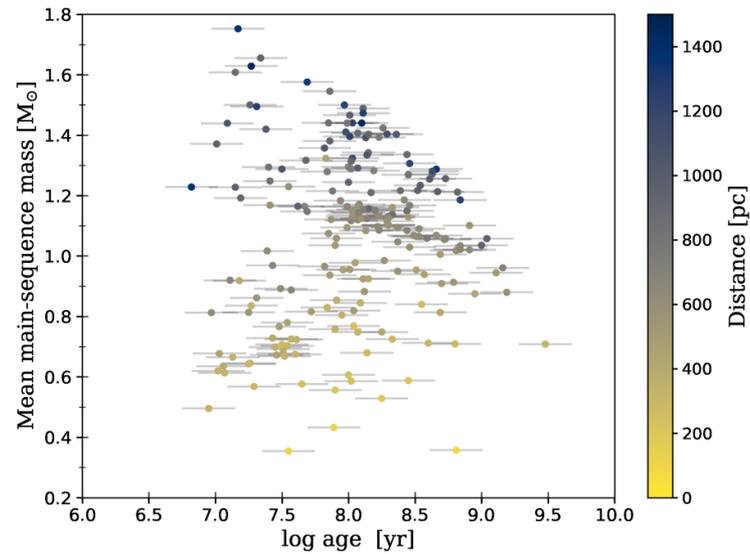
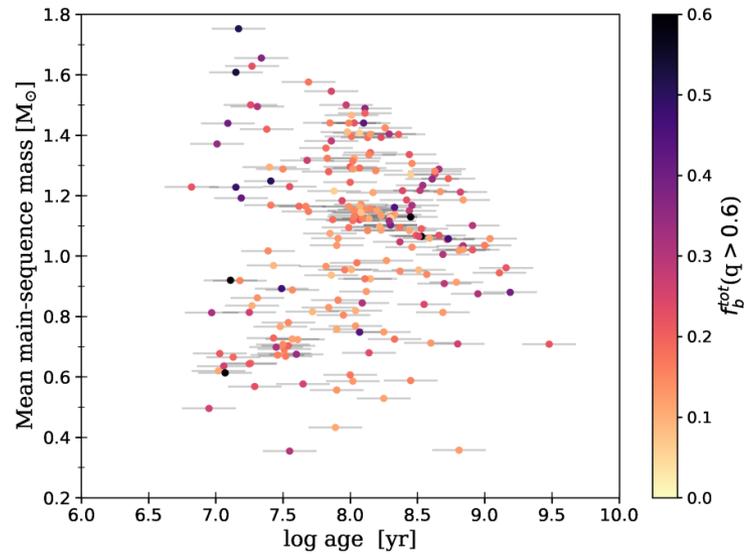
- Li, L., Shao, Z., Li, Z.-Z., et al. **2020**, ApJ, 901, 49
- Niu, H., Wang, J., & Fu, J. **2020**, ApJ, 903, 93
- Jadhav, V. V., Roy, K., Joshi, N., & Subramaniam, A. **2021**, AJ, 162, 264
- Li, L. & Shao, Z. **2022**, ApJ, 930, 44



Comparison of the unresolved multiplicity fraction values for the 10 OCs our study has in common with Jadhav, V. V. et al. 2021.

# Results and discussion

## 2) Dependence of the multiplicity fraction on the distance and stellar mass



The OC's parameters of age, distance, and mean sampled mass are heavily entangled: **complex selection effects**.

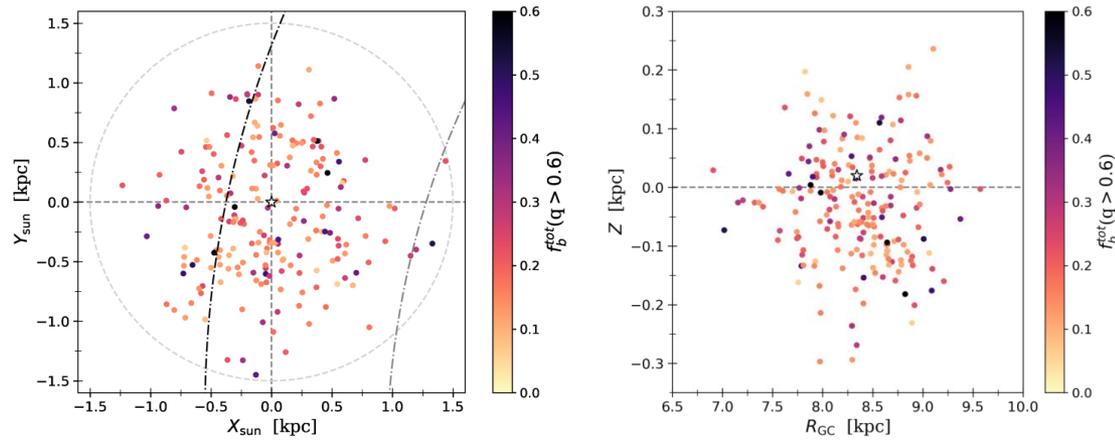
$f_b^{tot}$  increases with distance because for more distant OCs we tend to see only the upper ends of their MSs, which have more massive stars.



$f_b^{tot}$  increases with the mass of the primary star, in agreement with observational evidence from field stars and OCs (Bouvier, J., et al. 1997, A&A, 323, 139 and Deacon, N. R. & Kraus, A. L. 2020, MNRAS, 496, 5176).

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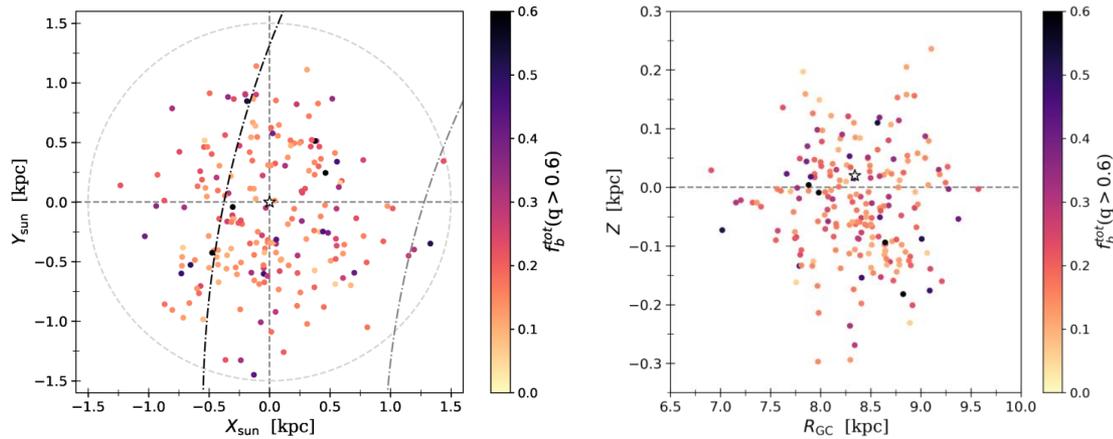
## 3) Dependence of the multiplicity fraction on position



There is no apparent correlation between  $f_b^{tot}$  and the position in or perpendicular to the Galactic plane.

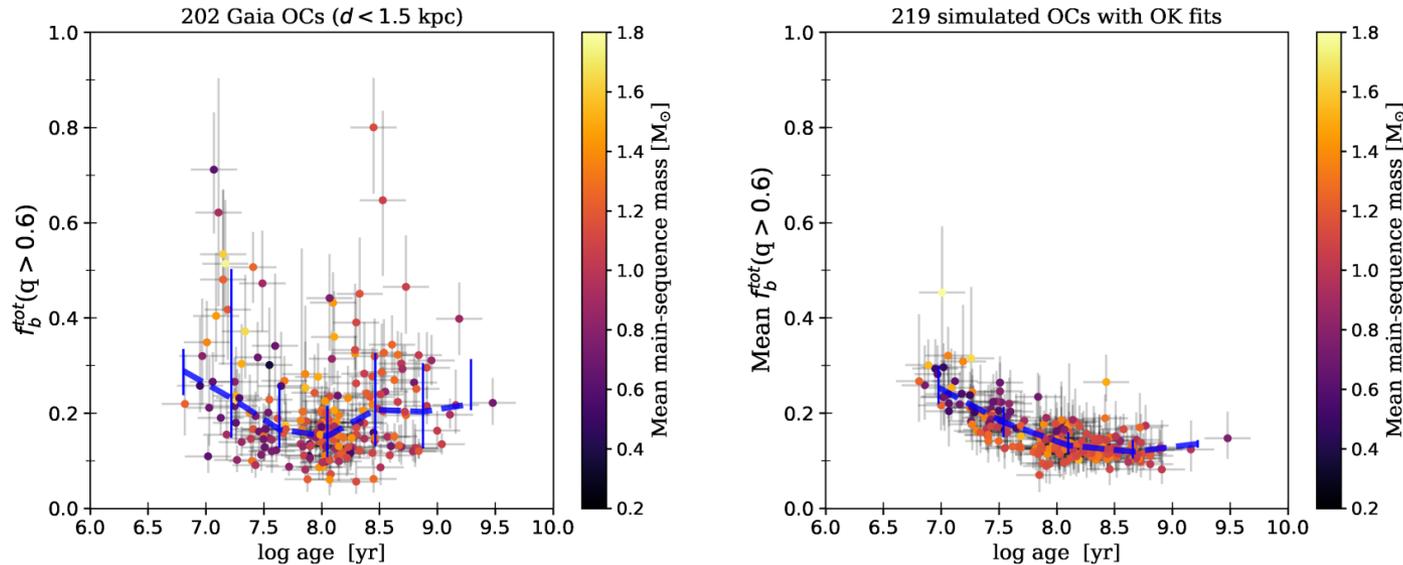
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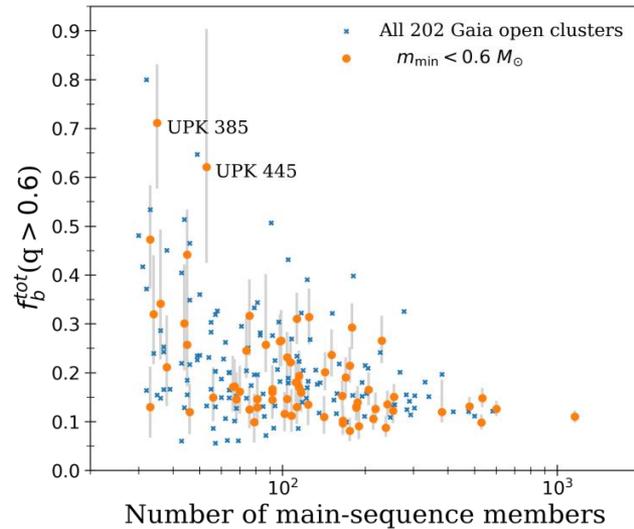
## 4) Dependence of the multiplicity fraction on the OC's age



Dividing the sample into four bins of mean main-sequence mass  $\langle m \rangle$  this age trend persists.

$f_b^{tot}$  running median trend (decrease with age until  $\sim 100$  Myr, and slight increase for older OCs) is reproduced by simulated OCs  $\Rightarrow$  mainly caused by the sample's complex selection effects.

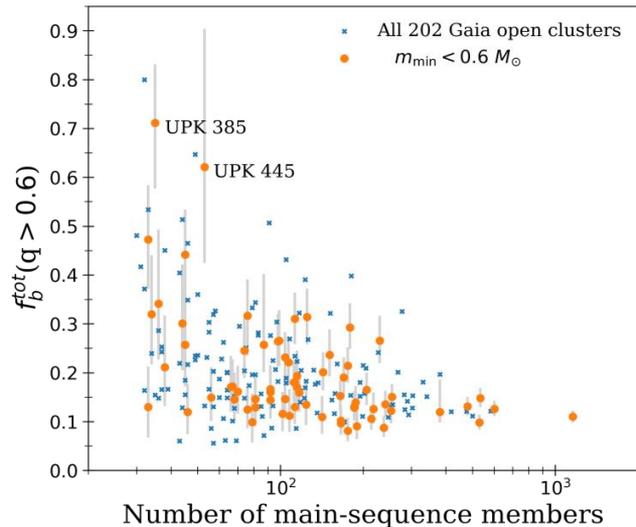
## 5) Dependence of the multiplicity fraction on the number of cluster members



OCs with

- $m_{\text{min}} < 0.6 M_{\odot}$  and
  - highly elevated multiplicity fractions
- could be candidates for being close to dissolution, in line with simulations (e.g. Hurley, J. R., Aarseth, S. J., & Shara, M. M. 2007, ApJ, 665, 707).

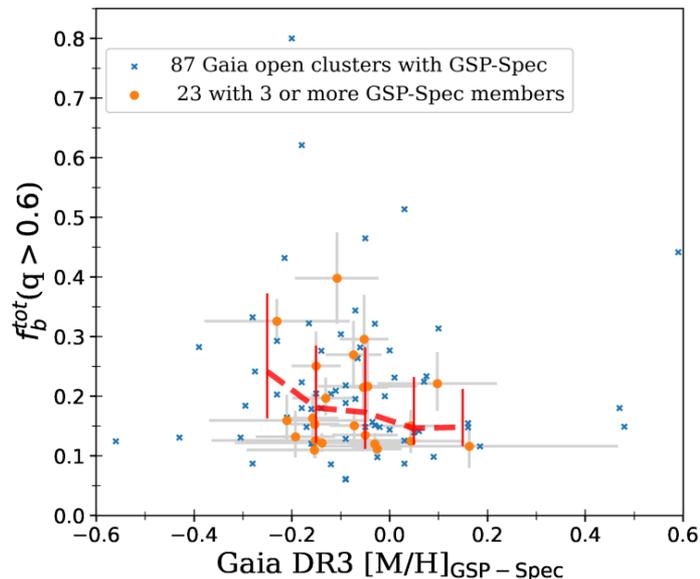
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## 6) Dependence of the multiplicity fraction on metallicity



*Gaia* DR3 GSP-Spec catalogue metallicities (Recio-Blanco, A., et al. 2022, A&A, in press, arXiv:2206.05541).

The **multiplicity fraction decreases with metallicity**, in line with recent studies using close binaries in the field (e.g. El-Badry, K. & Rix, H.-W. 2019, MNRAS, 482, L139 and Moe, M., Kratter, K. M., & Badenes, C. 2019, ApJ, 875, 61).

The same trend is found using Netopil, M., et al. 2022, MNRSS, Volume 509, Issue 1, pp.421-439, but for much less OCs.

## Conclusions

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- ✓ CMD is a fundamental diagnostic tool for OCs.
- ✓ The multiplicity fraction estimation depends inevitably to some degree on **modelling**.
- ✓ Our approach does not rely on fitting theoretical isochrones to the CMD, nor it depends on any stellar model.

The mixture model fitting is performed directly in *Gaia*'s observed CMD.

Synthetic CMDs are only used to characterise the  $q$  range that  $f_b$  takes into account and to estimate the total multiplicity fraction.

Our  $f_b$  is integrated over the main-sequence mass range of the OC: the OC's  $q$  distribution is not determined.

### Future work

Corroborate our results with revised and more complete membership lists:

Apply our method to the recent *Gaia* DR3 OC catalogue from Hunt, E. L. & Reffert, S., 2023, A&A, Volume 673, id.A114, 31 pp.